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Flow of DNA solutions in a microfluidic gradual contraction

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The flow of λ -DNA solutions in a gradual micro-contraction was investigated using direct measurement techniques. The effects on DNA transport in microscale flows are significant because the flow behavior is influenced by macromolecular conformations, both viscous and elastic forces dominate inertial forces at this length scale, and the fully extended length of the molecule approaches the characteristic channel length w_c (L/ $w_c \sim 0.13$). This study examines the flow of semi-dilute and entangled DNA solutions in a gradual planar micro-contraction for low Reynolds numbers $(3.7 \times 10^{-6} < \text{Re} < 3.1 \times 10^{-1})$ and high Weissenberg numbers (0.4 < Wi < 446). The semi-dilute DNA solutions have modest elasticity number, El = Wi/Re = 55, and do not exhibit viscoelastic behavior. For the entangled DNA solutions, we access high elasticity numbers $(7.9 \times 10^3 < \text{El} < 6.0 \times 10^5)$. Video microscopy and streak images of entangled DNA solution flow reveal highly elastic behavior evidenced by the presence of large, stable vortices symmetric about the centerline and upstream of the channel entrance. Micro-particle image velocimetry measurements are used to obtain high resolution, quantitative velocity measurements of the vortex growth in this micro-contraction flow. These direct measurements provide a deeper understanding of the underlying physics of macromolecular transport in microfluidic flow, which will enable the realization of enhanced designs of lab-on-a-chip systems. © 2015 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4929927]

I. INTRODUCTION

Lab-on-a-chip systems for biological applications such as DNA sequencing, hybridization, and pathogen detection will incorporate numerous microfluidic components and require the flow of macromolecules such as DNA, which may give the bulk fluid viscoelastic behavior. As compared to macroscale flows, the fully extended lengths of macromolecules approach the width of the fluid channels in microfluidic flows, and the small characteristic length scale of these devices leads to increasing influence of elastic and viscous forces. This is a unique flow environment that is not well understood. For viscoelastic flows, not only does the fluid flow influence the conformation of the macromolecule but also the presence of macromolecules affects the flow behavior. A deeper understanding of the viscoelastic flow behavior in micro-environments will enable optimized lab-on-a-chip system designs for enhanced sensing or rapid diagnostic applications.

Because complex fluids may display very different behavior in shear-dominated and extension-dominated flows, it is important to consider the variety of typical geometries that comprise lab-on-a-chip devices. Flow studies in microfluidic elements where the fluid experiences rapid changes to the flow area or flow direction are particularly valuable, since the spatial variation reveals the viscoelastic behavior.

This investigation examines viscoelastic flows in a microscale planar gradual contraction, a canonical microfluidic component. In this flow structure, as the fluid approaches the channel

from the upstream reservoir, it is spatially accelerated. The reservoir is concave with a large radius of curvature. There is nominal convex rounding at the channel entrance (radius of curvature of the rounding is much smaller than the channel width) due to the difficulty of obtaining sharp corners by microfabrication techniques.

Viscoelastic flows have been explored in other common microfluidic elements at negligible to moderate Reynolds (Re) number $(10^{-7} < \text{Re} < 10^2)$. Recent attention has been given to flows through microscale abrupt planar contraction geometries, since it is the microfluidic analog of the viscoelastic benchmark flow. In this geometry, an upstream channel of larger width suddenly contracts to a downstream channel of smaller width, resulting in sharp corners in the region of the contraction. A global characteristic of viscoelastic flow in abrupt microcontraction geometries is vortex growth and dynamics in the upstream channel with increasing flow rate. Studies have been conducted for flows of synthetic polymer solutions in abrupt micro-contraction-expansions (Rodd *et al.*, 2005, 2007; Lanzaro and Yuan, 2011, 2014; Li *et al.*, 2011a, 2011b) and DNA solutions in an abrupt micro-contraction (Gulati *et al.*, 2008). Additionally, there have been studies characterizing viscoelastic vortex dynamics in microbifurcations (Balan *et al.*, 2012) and in micro-bends (Gulati *et al.*, 2010), as well as utilizing viscoelastic instabilities in serpentine channels for micro-mixing (Burghelea *et al.*, 2004) and for micro-rectifier performance (Groisman and Quake, 2004; Jensen *et al.*, 2012).

Experimental and numerical studies in a related geometry to the gradual micro-contraction, a microfluidic planar hyperbolic contraction-abrupt expansion, have been reported recently. The hyperbolic contraction-abrupt expansion has a smoothly converging channel entrance but with convex curvature. It has been evaluated as an extensional micro-rheometer, since it enables nearly uniform strain rate along the channel centerline for geometries with high Hencky strains under Hele–Shaw flow conditions (Oliveira *et al.*, 2007). This geometry has also been used to characterize low viscosity, non-shear thinning (Boger) PAA solutions (Campo-Deano *et al.*, 2011) and for characterization of blood simulants (Sousa *et al.*, 2011) at small Re $(1 < \text{Re} < 10^2)$.

To our knowledge, experimental studies of viscoelastic flows in microscale planar gradual contractions have not been reported in the literature. Laminar flows through macroscale planar gradual contractions at small to moderate Re $(1 < \text{Re} < 10^4)$, however, have received some attention. Poole et al. (2005) explored flows of a moderately shear-thinning polyacrylamide (PAA) solution in a macroscale planar sudden expansion preceded by a gradual contraction. This geometry had a concave shape followed by significant convex curvature at the connection to the expansion; the radius of curvature of the concave shape was two times that of the convex. In the region of the gradual contraction, large velocities with large velocity gradients were observed near the sidewalls as compared with the smaller magnitude centerline velocity, leading to a velocity profile which they termed "cat's ears" due to the profile shape. The magnitude of the velocity overshoot (i.e., the difference between the velocity at the sidewalls compared with the centerline) in the plane with the flat sidewalls was found to be larger than the profiles in the plane with curved sidewalls of the contraction (Poole et al., 2005). Symmetric recirculation regions are only observed in the expansion portion of this device for viscoelastic flows. Threedimensional numerical simulations of viscoelastic flows in gradual planar contraction-abrupt expansion geometries modelled using the Phan-Thien-Tanner (PTT) model (Poole et al., 2007) and modelled by both the upper-convected Maxwell (UCM) and PTT model (Poole and Alves, 2009) qualitatively agreed with experimental observations of the "cat's ears" velocity effect.

In this investigation, λ -DNA serves as the biopolymer model because of its direct use in lab-on-a-chip applications and the extensive rheological characterization (LeDuc *et al.*, 1999; Perkins *et al.*, 1997). The molecular contour length L approaches the device length scale w_c; L/w_c ~ 0.13 for these flows. We explore flows of semi-dilute DNA solutions, where intermolecular interactions become important, and entangled DNA solutions and compare with the flows of a Newtonian fluid. While the flow field affects the conformation of the DNA at vanishing concentrations of DNA (Shrewsbury *et al.*, 2001; 2002), we show that the presence of the DNA affects the flow field only at sufficiently high concentrations and flow rates. Streak images were obtained to characterize the upstream flow kinematics to determine these critical conditions.

Pressure drops were measured to quantify the pressure drop due to the strong elastic flow behavior. Finally, micro-particle image velocimetry (μ PIV) was used to quantify the velocity fields of the recirculation region with high-resolution. It is hoped that these measurements will be used for validation of numerical simulations as well as to determine when viscoelastic effects are important in microflows of DNA.

II. EXPERIMENT

A. Device design and fabrication

Figure 1 contains a schematic and an image of the gradual contraction device. The device consists of two reservoirs connected by a 3.5 mm channel with rectangular cross-section, $130 \,\mu\text{m}$ wide and $50 \,\mu\text{m}$ deep. Arrows in Figure 1(a) indicate the fluidic path. Fluid enters through a through-hole located in the inlet reservoir approximately 0.5 cm upstream of the contraction. The fluid experiences contraction flow when accelerating from the converging reservoir into the straight channel. In the region nearest to the contraction, the converging shape is circular with radius of curvature of ~1800 μ m (Figure 1(b)). After traveling the length of the channel, the fluid exits the device through a through-hole in the outlet reservoir. The gradual contraction device was pre-loaded with distilled water under vacuum to remove all air bubbles from the system. Subsequently, the test fluid was delivered to the device.

The gradual contraction device was fabricated using conventional silicon microfabrication methods. A detailed description of the fabrication and bonding process flow are given by Shrewsbury et al. (2001); however, we provide a brief summary here. The device substrate was an n-type, 4 in. (100), single surface polished, silicon wafer. A 1 μ m layer of silicon dioxide was formed by wet oxidation of the wafer at 1100 °C for 3 h. Two photolithography sequences using a positive resist were performed to pattern first the contraction geometry and subsequently through-holes for external fluidic connection. In the first sequence, a thin layer of photoresist $(\sim 1.3 \,\mu\text{m})$ was spun on, exposed, and developed to create the device pattern and then the exposed silicon dioxide layer was etched using oxygen plasma. In the second photolithography step, a thicker layer of photoresist of $\sim 10 \,\mu m$ was spun on in order to protect the regions not to be etched during the subsequent etching of through-holes. The through-holes (1 mm diameter) that serve as the inlet and outlet located in the device reservoirs were patterned, developed, and then formed by a deep reactive ion etch (DRIE) through the thickness of the wafer. The photoresist mask was then removed, exposing the underlying silicon dioxide masking layer, and subsequent RIE created the 50 μ m deep device reservoirs and channels. Finally, the silicon dioxide layer was removed by buffered hydrofluoric acid.

A 170 μ m thick Pyrex[®] coverslip was bonded to the silicon wafer using epoxy, which enabled optical access for flow visualization. A 5–10 μ m thick layer of Epo-tek 301 epoxy (Epoxy Technology, Billerica, MA) was uniformly spun onto the coverslip, placed in contact with the etched silicon wafer, and cured. Oxygen plasma was directed into the device via the through-holes to ash away any unbonded epoxy. Finally, Tygon[®] 1/16 in. inner diameter

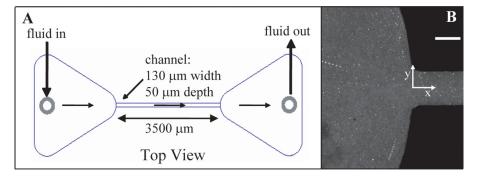


FIG. 1. (a) Top view of gradual contraction device. (b) Image of contraction region with a DNA solution $(40 \,\mu g/ml, Re = 0.314, Wi = 17.5, and El = 55)$ flowing through the device. Scale bar represents $100 \,\mu m$.

flexible tubing (Cole-Parmer) was affixed to the through-holes of both reservoirs on the backside of the device with a quick setting two part epoxy (J-B Kwik and J-B Weld) to provide the external fluidic connection to the device. A syringe pump is used to drive the flow during experiments.

B. Fluid rheology

Two viscoelastic DNA solutions of different concentrations were prepared as test fluids for this study using λ -DNA (New England Biolabs). λ -DNA has a molecular weight of 31.5×10^6 Da or 48 502 base pairs, a fully extended length of 17 μ m, and an equilibrium radius of gyration of 0.5 µm (Bustamante et al., 1994; Sanger et al., 1982; Verma et al., 1998). Additionally, the dynamics of this molecule in pure shear and pure extensional flow has been carefully documented (LeDuc et al., 1999; Perkins et al., 1997). Further, the conformational changes of λ -DNA at dilute concentrations in a similar microfluidic gradual contraction geometry (Shrewsbury et al. 2001, 2002) and the vortex growth of the higher concentration λ -DNA solutions in 2:1 abrupt contraction geometries (Gulati et al., 2008) have been characterized. The DNA solutions were diluted with $1 \times$ TAE buffer (40 mM Tris acetate and 1 mM EDTA, pH 8.3) to 40 μ g/ml and 400 μ g/ml DNA, respectively. In the absence of added monovalent salt, the polyelectrolyte nature of DNA will likely influence the dynamics and it is not anticipated that the solutions will behave as neutral synthetic polymer solutions. A similar influence is expected for our DNA solutions to those prepared at vanishing salt concentration conditions, resulting in an increased persistence length and hydrodynamic radius as compared with DNA in the fully screened high salt limit (Pan et al., 2014). Distilled water was tested as a Newtonian comparison.

In the previous work, we determined the overlap concentration c* of our DNA solution, the concentration where equilibrium coils begin to overlap each other, from the intrinsic viscosity by $c^* = 1/[\eta]$. The intrinsic viscosity can be estimated by the y-intercept of the plot of the reduced viscosity against the concentration in the low concentration limit (Shrewsbury et al., 2001). The reduced viscosity is the ratio of the specific viscosity and concentration or η_{sp}/c and the specific viscosity is given by $\eta_{sp} = (\eta - \eta_{sol})/\eta_{sol}$, where η_{sol} is the solution viscosity. This method gives an intrinsic viscosity $[\eta]$ of 0.01 ml/µg for DNA in TAE buffer and the overlap concentration $c^* = 1/[\eta] = 100 \,\mu$ g/ml (Gulati *et al.*, 2008). Other studies have defined overlap concentration by the expression, $c^* = M/[(4\pi/3)R_g^3N_A]$, where M is the molecular weight, R_g is the radius of gyration, and N_A is Avogadro's number. Using this definition, c* is approximately 40 μ g/ml for λ -DNA solutions under good solvent conditions (Hur et al., 2001; Pan et al., 2014). Hence, from the intrinsic viscosity and the direct estimate of c^* , the 40 μ g/ml DNA solution is found to be 0.4c* and 1c*, respectively, and the 400 μ g/ml DNA solution is 4c* and 10c*, respectively. As a result, the 40 μ g/ml DNA solution is classified in the semi-dilute (unentangled) regime $(0.5 < c/c^* < 3)$ and 400 µg/ml DNA in the entangled regime $(c/c^* > 3)$ (Pan et al., 2014). Additionally, as elaborated above, the equilibrium description of c* is used to describe the DNA solutions; however, it should be noted that under the high shear conditions explored in this study the dynamic chain overlap concentration c_s^* is expected to be a lower concentration than c* (Salamone, 1996).

The steady shear viscosity η and the first normal stress coefficient Ψ_1 for the 400 µg/ml DNA solution were characterized at 20 °C using a Malvern Bohlin Gemini rheometer and a Rheometrics RMS-800 mechanical spectrometer over the achievable shear rate range, 10^{-2} s⁻¹ < $\dot{\gamma}_c < 10^3$ s⁻¹. These material properties for the 400 µg/ml DNA solution are given in Figure 2. Both the viscosity η and the first normal stress coefficient Ψ_1 are highly shear-thinning. Steady shear viscosity for the 400 µg/ml DNA solution is fit to a Carreau model, $\eta = \eta_0 + (\eta_0 - \eta_\infty)[1 + (\Lambda \dot{\gamma})]^{(n-1)/2}$, where η_0 is the zero-shear rate viscosity, η_∞ is the infinite shear rate viscosity, n is the power law index, and Λ is a time constant. The fitted model parameters are $\eta_0 = 10$ Pa s, $\eta_\infty = 0.016$ Pa s, $\Lambda = 115$ s, and n = 0.121.

Dynamic rheological properties were determined by small amplitude oscillatory shear (SAOS) measurements using a Vilastic-3 Viscoelasticity Analyzer (Vilastic Scientific, Inc.), an

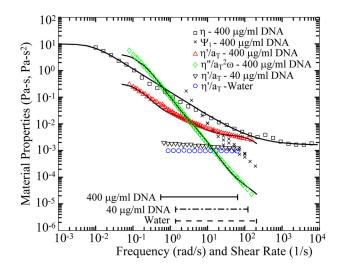


FIG. 2. Steady shear viscosity η and first normal stress coefficient Ψ_1 as a function of shear rate for 400 µg/ml DNA solution. Master curves of dynamic viscosity η'/a_T and dynamic rigidity $\eta''/a_T^{2}\omega$ at $T_{ref} = 20$ °C as a function of reduced frequency $a_T\omega$ for 400 µg/ml DNA solution. Also shown is the dynamic viscosity of the 40 µg/ml DNA solution and water as a function of frequency ω . The shear rate ranges ($\dot{\gamma}_c = V/(w_c/2)$) probed for these fluids through the gradual contraction device are indicated by the horizontal lines. The dynamic shear data are fit to a 3-mode Maxwell model; the parameters are given in Table I. The steady shear viscosity is fit to a Carreau model with parameters $\eta_0 = 10$ Pa-s, $\eta_{\infty} = 0.016$ Pa-s, $\Lambda = 115$ s, n = 0.121.

oscillatory flow capillary viscometer. SAOS measurements were taken at three temperatures T = 5, 10, and 20 °C, and combined into master curves at $T_{ref} = 20$ °C by time-temperature superposition using shift factors $a_T(5 °C) = 1.45$ and $a_T(10 °C) = 1.30$. The master curves of dynamic viscosity η'/a_T and dynamic rigidity $2\eta''/a_T^2\omega$ at $T_{ref} = 20 °C$ as a function of reduced frequency $a_T\omega$ for the 400 µg/ml DNA solution are shown in Figure 2. The dynamic viscosity of 40 µg/ml DNA and water at $T_{ref} = 20 °C$ are also given in Figure 2. The 40 µg/ml and 400 µg/ml DNA solutions were found to be mildly and highly shear-thinning, respectively, at high frequencies. The 40 µg/ml DNA solution viscosity is taken to be the maximum value of viscosity $\eta = 1.965 \times 10^{-3}$ Pa s, since it is only modestly dependent on shear rate.

The 400 μ g/ml DNA master curves of dynamic viscosity η'/a_T and dynamic rigidity $2\eta''/a_T^2\omega$ were fit to a multi-mode generalized Maxwell model describing the storage and loss moduli G' and G''

$$G''(\omega) = \sum_{i=1}^{N} \frac{g_k \lambda_k \omega}{1 + \lambda_k^2 \omega^2} \quad G'(\omega) = \sum_{i=1}^{N} \frac{g_k \lambda_k^2 \omega^2}{1 + \lambda_k^2 \omega^2} \,. \tag{1}$$

The relaxation spectrum λ_k and modulus parameters g_k are given in Table I for the three-mode best fit of the data. The relaxation time of the 400 μ g/ml DNA solution is taken as the longest relaxation time λ_1 . The relaxation time of the 40 μ g/ml DNA solution is calculated using the Rouse model given by

$$\lambda = \frac{[\eta]\eta_{sol}M}{RT},\tag{2}$$

TABLE I. Relaxation times and moduli for $400 \,\mu$ g/ml DNA.

k	λ_k (s)	g _k (Pa)
1	6.79	4.72×10^{-2}
2	0.259	$5.89 imes 10^{-2}$
3	0.005	$7.54 imes10^{-1}$

where $[\eta]$ is the intrinsic viscosity of the polymer solution, η_{sol} is the solution viscosity, M is the molecular weight of the polymer, R is the gas constant, and T is the temperature. The relaxation times for both DNA solutions are reported in Table II.

For flow visualization and μ PIV experiments of flows of 400 μ g/ml DNA solution and water, the test fluids are seeded with neutrally buoyant 1.0 μ m orange fluorescent polystyrene tracer particles (FluoSpheres[®], Molecular Probes). For flow visualization experiments, the water and 400 μ g/ml DNA were seeded at concentrations of 0.0125% by volume and 0.4% by volume, respectively. For μ PIV experiments, both solutions are seeded at concentrations of 0.4% by volume. At these volume fractions, $\phi_{0.0125} = 1.25 \times 10^{-4}$ and $\phi_{0.4} = 4 \times 10^{-3}$, by the Einstein expression, there is only a negligible increase in viscosity, $\eta = \eta_0 \{1 + 2.5 \phi_{0.4}\} = 1.01\eta_0$. Preliminary flow visualization of 40 μ g/ml DNA flow through the gradual contraction appears indistinguishable from water (cf. Figures 1(b), 6(c), and 6(b)) and hence, detailed pressure drop and μ PIV studies were not conducted for this fluid.

C. Dimensionless parameters

The microfluidic contraction flows in this study were characterized by three dimensionless parameters. The Reynolds (Re) number is defined as

$$\operatorname{Re}(\dot{\gamma}_c) = \frac{\rho V D_h}{\eta(\dot{\gamma}_c)} = \frac{2\rho Q}{(h+w_c)\eta(\dot{\gamma}_c)},\tag{3}$$

where $\eta(\dot{\gamma}_c)$ is the shear rate dependent viscosity, ρ is the solution density, $D_h = 2w_c h/(w_c + h)$ is the hydraulic diameter, $V = Q/(hw_c)$ is the average velocity, Q is the flow rate, $\dot{\gamma}_c = V/(w_c/2)$ is the characteristic shear rate, w_c is the channel width, and h is the channel depth. As with most microfluidic flows, the Re numbers accessed in this study are less than 1.

The Weissenberg (Wi) number is used to describe viscoelastic flows and is defined as

$$Wi = \lambda \dot{\gamma}_c = \frac{\lambda V}{w_c/2} = \frac{\lambda Q}{h w_c^2/2},\tag{4}$$

where λ is the relaxation time of the solution, taken as the longest Maxwell relaxation time for the 400 µg/ml DNA solution and the Rouse relaxation time for the 40 µg/ml DNA solution. Finally, the elasticity number (El) is the ratio of the dimensionless Wi to the Re

$$El = \frac{Wi}{Re} = \frac{2\lambda\eta(\dot{\gamma}_c)}{\rho w_c D_h} = \frac{\lambda(w_c + h)\eta(\dot{\gamma}_c)}{\rho w_c^2 h}.$$
(5)

Since the viscosity of the 40 μ g/ml DNA solution is only modestly dependent on shear rate, the maximum value of viscosity is used to compute the dimensionless parameters for all shear rates probed. Testing was conducted for flows of water, 40 μ g/ml DNA, and 400 μ g/ml DNA over the range of operating conditions given in Table III and the shear rate ranges probed are indicated by the horizontal lines in Figure 2.

TABLE II. Rheological properties at 20 °C.

	Relaxation time, λ (s)	Density, ρ (g/cm ³)	c/c*	Concentration regime
40 µg/ml DNA	0.133	1.007	0.4, ^a 1 ^b	Semi-dilute
$400\mu { m g/ml}$ DNA	6.79	1.000	4, ^a 10 ^b	Entangled

 $^{a}c^{*} = 100 \,\mu g/ml$ calculated from the intrinsic viscosity (Gulati *et al.*, 2008).

 ${}^{b}c^{*} = 40 \,\mu g/ml$ from Pan *et al.* (2014).

	Re	Wi	El
Water	0.015–0.926	0	0
40 µg/ml DNA	0.008-0.314	0.4-17.5	55
$400 \mu\text{g/ml}$ DNA	3.7×10^{-6} - 5.6×10^{-2}	2.2-446	$7.9 \times 10^{3} 6.0 \times 10^{5}$

TABLE III. Experimental operating space.

Experimental measurements in this study are also reported as dimensionless values. The non-dimensional pressure drop Δp is computed for water and 400 µg/ml DNA flows. At flow rate Q, $\Delta p(Q)$ is given by

$$\Delta \mathbf{p}(Q) = \frac{\Delta P(Q)}{\Delta P_{\rm sim}(Q)},\tag{6}$$

where $\Delta P(Q)$ is the measured pressure drop for water or the 400 µg/ml DNA solution at flow rate Q and $\Delta P_{sim}(Q)$ is the simulated pressure drop for a Newtonian fluid or for an inelastic, shear-thinning fluid at flow rate Q, respectively. The simulated pressure drops are calculated from three-dimensional finite element simulations of a Newtonian fluid with viscosity of water and a fluid with identical Carreau model parameters describing the steady shear viscosity of the 400 µg/ml DNA solution and provided the viscous contribution to the pressure drop. Hence, Δp uncovers the significance, if any, of the elastic contribution to the total pressure drop for 400 µg/ml DNA over the range of flow rates.

Additionally, the dimensionless vortex reattachment length χ is given as follows:

$$\chi = \frac{L_V}{w_c},\tag{7}$$

where the vortex length L_V is the arc length along the upstream channel wall between the boundary of the secondary flow vortex and the contraction plane and w_c is the channel width.

Spatial positions are reported using x as the axial coordinate and y as the transverse coordinate. The origin is set at the x-position at the contraction plane, where the converging, upstream reservoir meets the downstream rectangular channel, and the y-position at the centerline of the device. The normalized x- and y-positions are given by $x' = x/w_c$ and $y' = y/w_c$. The normalized x- and y-velocities are given by v_x/V and v_y/V , respectively.

D. Pressure drop measurements

A schematic of the pressure measurement set-up is shown in Figure 3(a). The pressure drop is measured across the entire micro-contraction device using a flow-through pressure sensor (Honeywell Micro Switch 26PCA) with a nominal pressure range of 1 psi. The voltage

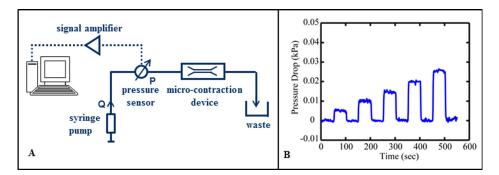


FIG. 3. (A) Schematic of the pressure measurement setup. (b) Pressure drop for flow of water through gradual contraction demonstrating the transient response of the system as the flow rate is stepped from 5 to 25 μ l/h in five equal increments of 5 μ l/h and in between dropped to 0 μ l/h.

signal from the pressure transducer is amplified by an instrumentation amplifier and subsequently recorded to a 12 bit I/O board on a computer. The sensor is placed in the tubing just upstream of the device. Upstream of the sensor, a syringe pump delivers the fluid to the micro-contraction device at controlled volumetric flow rates. The outlet flow from the micro-contraction is directed to a waste reservoir at atmospheric pressure. The measured pressure drops are dominated by the pressure drop through the straight channel but contain contributions from the gradual contraction and expansion regions and a minuscule contribution from the connected tubing.

Pressure drops were measured for flows of water and $400 \,\mu g/ml$ DNA. For water flow through the gradual contraction, a commercial syringe pump (Cole-Parmer 40900) with a $1000 \,\mu$ l volume glass syringe is used to mechanically control the flow rate over the testing range, $5 < Q < 300 \,\mu$ l/h. For 400 μ g/ml DNA flow through the gradual contraction, a custom syringe pump with a $10\,\mu$ l volume glass syringe is used to deliver flows over the range, $0.5 < Q < 40 \,\mu$ l/h. The syringe sizes were chosen in order to maximize the plunger velocity and glass syringes were chosen so that the fluids could be delivered as smoothly as possible. Data were acquired at 300 Hz and the average value was reported each second. The pressure drop is computed as the difference between the mean steady-state values at zero flow (over a minimum of 60 s) and at the flow rate of interest (over a minimum of 100 s). The difference was taken to account for any slight drift in the transducer signal that may have occurred over the duration of testing. The transient response was recorded but not included in the differential pressure drop calculation. Between runs, the system was brought to rest and pressure measured for a minimum of 60 s in order to check that the device was operating properly (i.e., no clogs or leaks were present). The transient response of the pressure system for flows of water in the micro-contraction device is shown in Figure 3(b). The system response time to steady-state is rapid and on the order of seconds.

E. Visualization techniques

The steady flow kinematics in the region of the contraction (in the reservoir upstream of the straight channel) for flows of water and 400 μ g/ml DNA are investigated using video microscopy, streak imaging, and μ PIV. An inverted epifluorescence microscope equipped with either a 20×/ 0.5 NA Plan objective lens, a $10 \times / 0.3$ NA Universal Plan objective lens, or a $4 \times / 0.13$ NA Universal Plan objective lens was used for flow visualization measurements. For water flows, a mercury burner served as a constant illumination source for streak imaging and two alternating Nd:YAG lasers, with a wavelength of 532 nm and each firing at 15 Hz for a pulse duration of ~6 ns, illuminated the flow for μ PIV imaging. For 400 μ g/ml DNA flows, the two alternating Nd:YAG lasers were illumination sources for both streak imaging and μ PIV. Lasers were used as the illumination source for 400 μ g/ml DNA flows because the images obtained were sufficient to produce high quality streak images. Images with 1013×1000 pixels were captured using a progressive scanning full-frame shutter camera (Pulnix TM-9701) and recorded to a computer for post-processing. All images were obtained at the midplane of the channel (25 μ m from the top and bottom of the device) at $20\times$, $10\times$, or $4\times$ magnifications depending on the size of the vortex. Streak imaging and μ PIV analyses were not conducted for 40 μ g/ml DNA flows because initial visualization studies using the two alternating Nd:YAG lasers across the range of operating conditions given in Table III did not reveal kinematic differences from water.

The external connections to the micro-contraction were identical to the pressure measurement setup except there is no pressure sensor placed in the upstream tubing. A commercial syringe pump (Cole-Parmer 40900) was used to control the volumetric flow rate over the range, $2 < Q < 100 \mu l/h$, for visualization experiments. A 1000 μl volume glass syringe was used with the syringe pump. As with the pressure measurements, in between runs, the flow was turned off for a minimum of 60 s and then allowed to flow for a minimum of 60 s to ensure steady-state behavior prior to image acquisition.

Streak images were constructed by overlaying 4 s of sequential images taken at either $4 \times$ or $10 \times$ magnification of the steady flow taken at 30 fps using Scion Image Beta 4.0.2 image

processing software. For μ PIV measurements, the lasers are controlled independently to fire at given time intervals, ranging from 0.2 ms to 33 ms, in order to optimize the particle displacements for high quality cross-correlation μ PIV algorithms. For each flow rate tested, 300 image pairs were collected for μ PIV analysis at either 10× or 20× magnification, depending on the size of the vortex. The size of interrogation regions were chosen such that they contained a minimum of 8 particles per region and the displacements were chosen to be less than 33% the length of the interrogation region in the axial and transverse directions. For the flows of water, this corresponded to the regions closest to the contraction where the fluid was rapidly accelerating. For 400 μ g/ml DNA flows, the focus was on the kinematics within the vortex region and the timing intervals were chosen to optimize the displacements in fast flow region towards the outer edge of the vortex. The primary flow was significantly faster than the secondary flow, and consequently the timing and interrogation region sizes optimized for the vortex region resulted in spurious cross-correlation vectors in the primary flow and were subsequently removed. Additionally, spurious vectors in the regions past the wall where there was no flow (for the silicon substrate) were removed for both water and 400 μ g/ml DNA velocity fields. Individual velocity fields constructed from single image pairs were ensemble averaged over all 300 pairs of images to construct an averaged velocity vector field.

Numerous factors in the visualization system setup contribute to accuracy and resolution of post-processed images. For our measurement system, we have previously reported measurement depth δz_m (Meinhart *et al.*, 2000) because it more accurately reflects the depth of the image plane as compared to the depth of field. The measurement depth is given by

$$\delta z_m = \frac{3n\lambda_0}{\left(NA\right)^2} + \frac{2.16d_p}{\tan\theta} + d_p,\tag{8}$$

where λ_0 is the wavelength of the imaged light, *n* is the refractive index, *NA* is the numerical aperture, d_p is the tracer particle diameter, and $\theta = \sin^{-1}(NA/n)$. For this imaging system, $\lambda_0 = 560$ nm, n = 1.33, $d_p = 1 \,\mu$ m, and NA = 0.5, 0.3, and 0.13 for the 20×, 10×, and 4× magnifications, respectively. Hence, for this study, δz_m is 15.3 μ m or 28% of the channel depth for the 20× objective lens, δz_m is 35.2 μ m or 64% of the channel depth for the 10× objective lens, and δz_m is 155 μ m or over 100% of the channel depth for the 4× objective lens. Additionally, uncertainty also arises in applying the cross-correlation algorithm over parts of the flow field where particle movement within interrogation regions is not spatially uniform, such as at the interface between the primary and secondary flow regions and nearby walls. Ensemble averaging was used to minimize uncertainty due to poor correlations.

F. Computational fluid dynamics simulations

Three-dimensional numerical simulations were conducted using Comsol Multiphysics 3.2 in order to model the flow of a Newtonian fluid with the viscosity of water and a Carreau fluid with the same shear-thinning behavior as the $400 \,\mu g/ml$ DNA solution. The non-dimensional momentum equations were used to simulate the fluid flow in the channel downstream of the gradual micro-contraction. Simulations were performed at the same flow rates as experimental pressure drops across a portion of the total channel length where the flow is fully developed. For the simulations, the walls were specified as no-slip boundaries, the average velocity was specified as the inlet boundary condition for each flow rate, and the pressure was set to zero at the outlet boundary. The simulated pressure drop was then scaled for the total channel length of 3500 μ m in order to determine the total channel pressure drop experienced by water and the Carreau fluid. Finally, the non-dimensional pressure drop was computed (cf. Eq. (6)).

III. RESULTS AND DISCUSSION

A. Pressure drop measurements

The measured steady-state pressure drops for water and 400 μ g/ml DNA flows in the gradual contraction device are given in Figure 4. The pressure drop relationships for water and

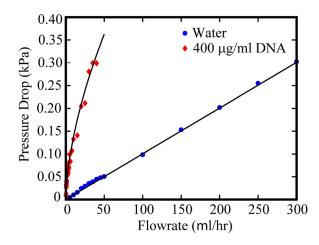


FIG. 4. Pressure drop for flow of water and 400 μ g/ml DNA through gradual contraction device as a function of flow rate Q. The pressure drop for water follows the functional form, $\Delta P = 0.001Q$, and the pressure drop for 400 μ g/ml DNA follows the functional form, $\Delta P = 0.035Q^{0.6}$.

400 μ g/ml DNA are given by the functional forms, $\Delta P = 0.001Q$ and $\Delta P = 0.035Q^{0.6}$, respectively. The dimensionless pressure drop Δp of water is computed as the ratio of the measured pressure drop and the simulated pressure drop over the channel region for water as given in Eq. (6). The Δp for water as a function of flow rate is given in Figure 5(a). The error bars indicate the uncertainty in Δp measurements, which are propagated from the uncertainty in the differential pressure drop, estimated as 0.017 kPa or 0.25% of the range of the pressure sensor.

For water flow, $\Delta p \sim 1.1$ for the higher flow rates, $Q > 50 \,\mu$ l/h (Figure 5(a)). The portion of Δp above unity (~10% of the simulated channel pressured drop ΔP_{sim}) is expected to contain the pressure contributions from the turn and expansion flow at the tubing entrance to the upstream inlet reservoir, the gradually converging upstream reservoir that joins the channel at the contraction plane, and the gradually expanding outlet reservoir. A range of Δp from 1.05 to 1.3 are obtained for the slower flows with notably high error uncertainty due to the measured pressure drops falling below or being close in magnitude to the uncertainty from the pressure sensor. Additionally, the nature of the drive mechanism of the syringe pump and the short duration of the test may have produced slightly elevated flow rates than expected, resulting in higher Δp .

In a similar manner, the Δp for 400 μ g/ml DNA is computed as the ratio of the measured pressure drop of 400 μ g/ml DNA flow and the simulated pressure drop over the channel region for a fluid with an identical Carreau model viscosity relationship to the 400 μ g/ml DNA

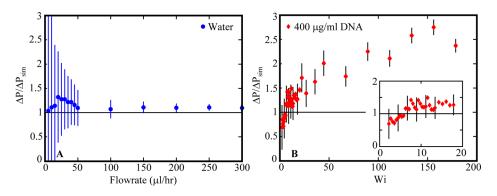


FIG. 5. Dimensionless pressure drop $\Delta P/\Delta P_{sim}$ for flow of (a) water as a function of flowrate and (b) 400 µg/ml DNA through gradual contraction device as a function of Wi. Error bars indicate the uncertainty in $\Delta P/\Delta P_{sim}$ propagated from the uncertainty in the differential pressure drop measurements. Inset in (b) is the dimensionless pressure drop of 400 µg/ml DNA at low Wi with some representative error bars included.

solution (Eq. (6)). Recasting pressure drops as Δp isolates the viscoelastic contributions from the contraction and expansion regions (i.e., the tubing entrance to the inlet, the inlet reservoir, and outlet reservoir) of the microdevice. The dimensionless pressure drop as a function of Wi is given in Figure 5(b). As Wi approaches zero, we expect Δp for 400 µg/ml DNA to approach 1.1 as was observed for the Newtonian case. Additionally, viscous behavior would dominate the DNA solution flow at this Wi limit. For Wi < 5.8, Δp falls below this asymptote. The measured pressure drops in this Wi range are close in magnitude to the uncertainty from the pressure sensor, yielding large error uncertainty. Moreover, the flows are very slow (0.5 µl/h < Q < 1.3 µl/h) and smooth, consistent flow may have been difficult to achieve with the syringe pump and throughout the device. For 6 < Wi < 18, Δp remains between 1.1 and 1.3, and for Wi > 20, Δp increases with Wi until reaching a plateau value of $\Delta p \sim 2.75$ at high Wi. The saturation of Δp in our work, as was previously suggested by Rodd *et al.* (2005), is likely a consequence of polymer chains reaching their finite extensibility limit.

The growth and asymptotic approach of Δp with increasing Wi can be compared with the previously reported micro-contraction flows. The growth mostly closely resembles the results of Rodd *et al.* (2005), in which a plateau of slightly higher magnitude ($\Delta p \sim 3.5$) was observed for flows of semi-dilute, mildly shear thinning 3.5c* PEO solutions in a 16:1:16 abrupt planar contraction-expansion over a wider Wi range. Additionally, the plateau magnitude is slightly lower than the maximum value reported in our past studies in a 2:1 abrupt micro-contraction of $\Delta p \sim 3.5$ for flow of the same DNA solution over a wider Wi range, although there is no plateau observed for the 2:1 abrupt contraction flow (Gulati *et al.*, 2008). The Δp maximum in the gradual micro-contraction is larger than the reported peak values of $\Delta p \sim 2.15$ and ~ 2.0 for flows of mildly shear-thinning semi-dilute 15c* and 20c* PEO solutions, respectively, in 8:1:8 contraction-expansion over a similar Wi range (Li *et al.*, 2011a) and peaks of $\Delta p \sim 1.8$ for weakly shear-thinning 8.3c* PAA solution flows in an 8:1:8 contraction-expansion and 3.3c* PAA solution flows in a 16:1:16 contraction-expansion over a similar Wi range (Lanzaro and Yuan, 2011).

B. Flow visualization

Streak imaging techniques were used to elucidate fluid pathlines in the reservoir upstream of the channel (Figure 6). These were taken at the lowest magnification $(4\times)$ in order to view the regions on both sides of the channel centerline. For flows of distilled water, no vortices are present across the range of Re probed. Examples of the streak images obtained for water are given in Figures 6(a) and 6(b) for flow at Re = 0.08 and Re = 0.31, respectively. However, symmetric, stable vortices are observed in streak images for flows of $400 \,\mu\text{g/ml}$ DNA at Re = 5.2×10^{-3} , Wi = 112, and El = 2.1×10^{4} and Re = 1.8×10^{-2} , Wi = 223, and El = 1.3×10^{4} (Figures 6(c) and 6(d)) illustrating the strong elastic flow behavior. These vortices grow dramatically with increasing Re and Wi and do not exhibit time-dependence across the Wi range probed.

Although detailed streak images are not reported here, it should be noted that video microscopy revealed no recirculation across the Re and Wi range for $40 \mu g/ml$ flows in the gradual contraction, indicating non-elastic behavior (cf. Figure 1(b) and Figures 6(a) and 6(b)). This is consistent with the observations of non-shear thinning fluids in other planar geometries. Vortices are not present for experimental flows of Boger (non-shear thinning) fluids in *macroscale* planar abrupt contractions, whereas vortex growth occurs for shear-thinning fluids (Nigen and Walters, 2002; Evans and Walters, 1986). Similarly, flows of non-shear thinning dilute PEO solutions in a *microscale* abrupt planar bend show the absence of vortices, while concentrated semi-dilute solutions of the same PEO, which have shear thinning behavior, exhibit elastic vortex growth (Gulati *et al.*, 2010). Additionally, the chain rigidity of the DNA molecule may play a role in the lack of vortex dynamics. Arratia *et al.* (2006) do not observe an elastic instability for dilute solutions of flexible PAA reveal flow instability (Arratia *et al.*, 2006).

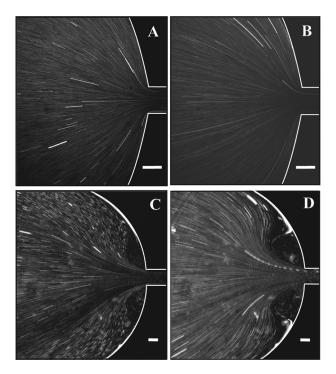


FIG. 6. Streak images of a microscale gradual contraction device for flows of water at (a) Re = 0.08 and (b) Re = 0.31 and $400 \,\mu$ g/ml DNA at (c) $Re = 5.2 \times 10^{-3}$, Wi = 112, and $El = 2.1 \times 10^4$ and (d) $Re = 1.8 \times 10^{-2}$, Wi = 223, and $El = 1.3 \times 10^4$. Each scale bar represents 100 μ m.

C. Evolution in vortex length

The vortex length L_V was obtained by measuring the arc length along the wall from the edge of the vortex boundary to the corner of the contraction in pixels. The size of the vortex above the centerline was determined from digital microscopy videos taken at the higher magnifications. The length in pixels was then converted to a dimensional length scale (1 pixel = $2.26 \,\mu$ m for $20 \times$ magnification and 1 pixel = $1.13 \,\mu$ m for $10 \times$ magnification). Dimensionless vortex length χ was computed using Eq. (7). Figure 7 shows the relationship between χ and Wi for flows of $400 \,\mu$ g/ml DNA. The increase in the dimensionless vortex length is well described by $\chi = 0.43$ (Wi – Wi_{crit})^{0.45} where Wi_{crit} is 8.9 over the Wi range 8.9 <Wi < 446. At low Wi, no vortex was present, consistent with expected behavior for Newtonian flow (cf. streak image of water flow in Figure 9(a)). The onset and growth of vortices occur in the range 8.9 <Wi < 22.

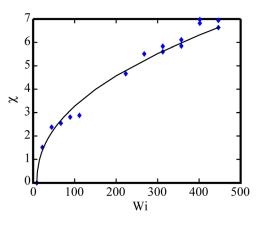


FIG. 7. Average dimensionless vortex length for flows of $400 \,\mu$ g/ml DNA through gradual micro-contraction device as a function of Wi. The vortex length follows the functional form, $\chi = 0.43$ (Wi - Wi_{crit})^{0.45} where Wi_{crit} is 8.9.

It is difficult to make comparisons of vortex growth with the previous studies of viscoelastic flows in micro-contractions due to the unique continuously converging shape of the gradual micro-contraction. Hyperbolic micro-contractions provide the closest comparison given their converging shape though the contraction is preceded by a straight channel section where the vortex develops. The non-dimensional vortex length χ_u is calculated as the ratio of the vortex length (measured along the straight section) and the upstream width w_u . If we recast the dimensionless vortex length (the arc length of vortex) for our 400 μ g/ml DNA flows in the gradual micro-contraction by an estimate of the upstream width of the reservoir of 2000 μ m (the width of the gradual contraction that is visible in the images at the lowest magnification), the vortex grows to a maximum $\chi_u = 0.45$. The size and growth of the vortex are similar to flows of moderately shear-thinning xanthan gum solutions in hyperbolic contractions (Hencky strains, $\varepsilon_H = \ln(w_u/w_c) = 2$ and 3) across a similar Wi range (Sousa *et al.*, 2011).

D. Micro-particle image velocimetry

Velocity vector fields for flows of water and 400 μ g/ml DNA through the gradual microcontraction were obtained by μ PIV techniques. A series of 300 image pairs were taken and flow fields for all pairs of images are averaged to construct the velocity vector field. Images are obtained at 20× magnification for water flow and 400 μ g/ml DNA at low Wi, where no or small vortices are present. For 400 μ g/ml DNA flows at higher Wi where larger vortices are present, images are obtained at 10× magnification. The interrogation regions at 10× and 20× magnification are ~28 × 28 μ m and ~14 × 14 μ m, respectively, with a 50% overlap.

Figure 8 shows the velocity field for water flow at Re = 0.31 above the centerline of the gradual micro-contraction. Figure 9 contains velocity fields for flows of 400 µg/ml DNA in the recirculation region at low Wi (Wi = 8.9 and 67). The contraction is located at x' = 0 and the centerline is located at y' = 0. For 400 µg/ml DNA flows in the gradual micro-contraction, no recirculation is observed for the low Wi case and the transition to vortices (i.e., to elastic flow behavior) occurs at Wi > 8.9. Figure 10 indicates the dramatic vortex growth with increasing

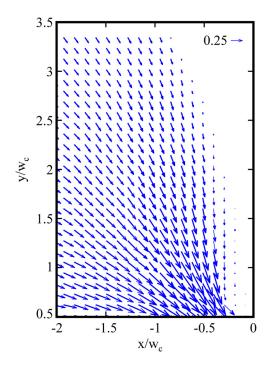


FIG. 8. Velocity vector field for water flow at Re = 0.31 through gradual contraction. The contraction is located at x' = 0 and the centerline is located at y' = 0.

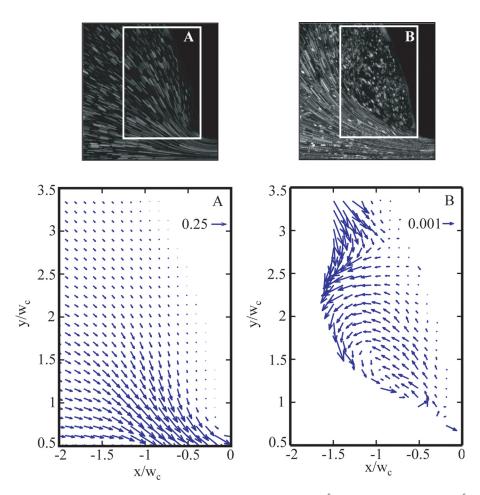


FIG. 9. Velocity vector fields for $400 \,\mu$ g/ml DNA flow at (a) Re = 5.0×10^{-5} , Wi = 8.9, and El = 1.8×10^{5} and (b) Re = 2.1×10^{-3} , Wi = 67, and El = 3.2×10^{4} through gradual contraction. The corresponding streak images and region of interest are shown at top.

Wi for flows of $400 \,\mu\text{g/ml}$ DNA in the gradual micro-contraction. The flow conditions shown in Figure 10 are (a) Wi = 8.9, (b) Wi = 67, (c) Wi = 223, (d) = 268, and (e) Wi = 312.

The normalized x- and y-velocity profiles for $400 \,\mu\text{g/ml}$ DNA flow (Wi = 268) at the x-position of the vortex center (x' = -1.77) is given in Figure 11. The y-position of the vortex center is y' = 1.45, where the normalized x- and y-velocities, v_x/V and v_y/V, both experience a zero velocity within the μ PIV spatial resolution. Figure 12 shows the evolution of the normalized x- and y-positions of the vortex center with increasing Wi. The error bars correspond to the spatial resolution of the interrogation regions (normalized by the channel width) used to construct the velocity fields. With increasing Wi, the vortex center moves farther into the upstream reservoir, with shifts of greater magnitude in the axial direction compared with the transverse direction.

It is hoped that the experimental velocity fields constructed in the vortex region demonstrate the use of μ PIV for quantitative validation of computational design tools. Preliminary comparisons to simulations have been presented elsewhere (Nonaka *et al.*, 2005; Trebotich *et al.*, 2005).

IV. CONCLUSION

The small length scales and high shear rates characteristic of polymer flow in microfluidic structures enable access to very high elasticity numbers, which are unable to be explored at the macroscale. In this flow environment, high Weissenberg number and very low Reynolds

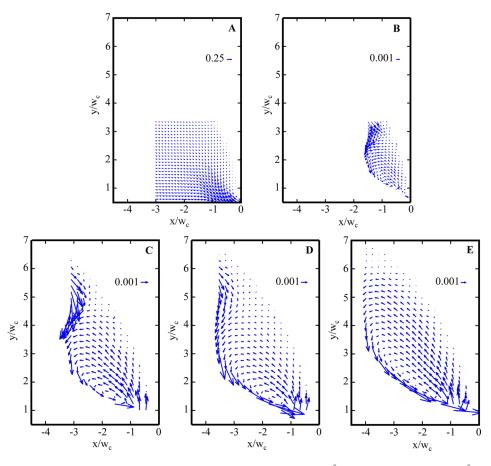


FIG. 10. Velocity vector fields for $400 \,\mu$ g/ml DNA flow at (a) Re = 5.0×10^{-5} , Wi = 8.9, and El = 1.8×10^{5} and (b) Re = 2.1×10^{-3} , Wi = 67, and El = 3.2×10^{4} ; (c) Re = 1.8×10^{-2} , Wi = 223, and El = 1.3×10^{4} ; (d) Re = 2.4×10^{-2} , Wi = 268, and El = 1.1×10^{4} ; and (e) Re = 3.1×10^{-2} , Wi = 312, and El = 1.0×10^{4} through gradual contraction.

number flows are simultaneously attained. DNA flows in a gradual micro-contraction geometry were characterized via experimental measurements of pressure drops, visualization of the flow kinematics, and velocity fields using μ PIV.

The flow of semi-dilute (unentangled) and entangled DNA solutions of modest and high El respectively were investigated over a range of low Re $(3.7 \times 10^{-6} < \text{Re} < 3.1 \times 10^{-1})$ and high

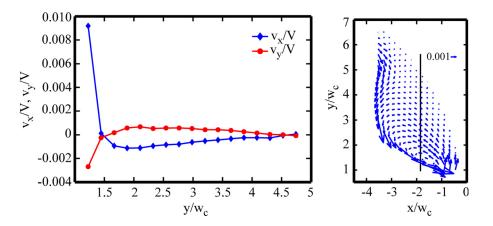


FIG. 11. Normalized velocity profiles for 400 μ g/ml DNA flow (Re = 2.4 × 10⁻², Wi = 268, and El = 1.1 × 10⁴) through the gradual contraction at the x-position of the vortex center (x' = x/w_c = -1.77, corresponding velocity field at right). Velocities are normalized by the average velocity in the downstream channel. The connected lines are to guide the eye.

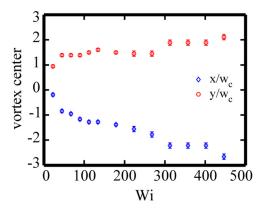


FIG. 12. Evolution of the vortex center for flows of $400 \,\mu$ g/ml DNA through the gradual contraction as a function of Wi. The error bars correspond to the spatial resolution of the interrogation regions (normalized by the channel width) used to construct the velocity fields.

Wi (0.4 < Wi < 446). The semi-dilute DNA flows are constant El = 55 and the entangled DNA solution flows probe the El range, $7.9 \times 10^3 < El < 6.0 \times 10^5$. Preliminary flow visualization experiments indicated no vortex behavior for flows of the non-shear-thinning semi-dilute DNA solutions over the entire parameter range probed. For flows of the entangled DNA solutions, strong, steady, symmetric vortex growth is observed for increasing Re and Wi. The dimensionless vortex length χ is quantified as a function of Weissenberg number; it is well described by a power law of the form $\chi = 0.43(Wi - Wi_{crit})^{0.45}$ where Wi_{crit} is 8.9. Dimensionless pressure drops Δp are also determined for the entangled DNA flows which reach a peak value of 2.75 at around Wi ~ 155. Finally, velocity fields constructed using μ PIV quantify the vortex dynamics from Newtonian-like flow at low Wi to the onset of vortex activity and dramatic growth with increasing Wi.

It is hoped that these direct measurements will be useful for forming comparisons with numerical simulation for optimization of lab-on-a-chip designs incorporating macromolecular flows. Additionally, these measurements of macromolecular flow in microfluidic geometries reveal the fundamental physics of this unique flow environment where the molecular lengths approach the critical device lengths ($L/w_c \sim 0.13$). The issue of molecular confinement and the influence of molecular concentration on flow are particularly relevant concerns for realistic design and operation of lab-on-a-chip applications incorporating macromolecular flows.

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