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A Comparative Study of Threshold-based Feature Selection Techniques

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Abstract

Given high-dimensional software measurement data, researchers and practitioners often use feature (metric) selection techniques to improve the performance of software quality classification models. This paper presents our newly proposed threshold-based feature selection techniques, comparing the performance of these techniques by building classification models using five commonly used classifiers. In order to evaluate the effectiveness of different feature selection techniques, the models are evaluated using eight different performance metrics separately since a given performance metric usually captures only one aspect of the classification performance. All experiments are conducted on three Eclipse data sets with different levels of class imbalance. The experiments demonstrate that the choice of a performance metric may significantly influence the results. In this study, we have found four distinct patterns when utilizing eight performance metrics to order 11 threshold-based feature selection techniques. Moreover, performances of the software quality models either improve or remain unchanged despite the removal of over 96% of the software metrics (attributes).

Keywords: performance metrics, threshold-based feature selection technique, software metrics, classification.

1 Introduction

Given a set of software metrics (independent features or attributes) the objective of feature selection is to remove irrelevant or redundant features, which can then be discarded from the analysis. Reducing the number of features in a data set can lead to faster model training and improved classifier performance. Feature selection has been widely used and thoroughly researched [6, 7, 10]. The two general categories for feature selection are *filters* and *wrappers*. Filters are algorithms in which a feature subset is selected without involving any learner. Wrappers are algorithms that use feedback from a learning algorithm to determine which feature(s) to include in building a classification model. An-

other categorization for feature selection techniques is *feature ranking* and *feature subset selection techniques*. Feature ranking ranks the attributes according to their individual predictive power, while feature subset selection selects subsets of attributes that collectively have good predictive power. We consider filter-based feature ranking techniques in this study.

In this paper, we present our newly proposed threshold-based feature selection techniques (TBFS) which represent a substantial extension of the FAST algorithm proposed by Chen and Wasikowski [2]. Our technique is much more general than that of Chen and Wasikowski. Their procedure calculates a ROC curve by discretizing the distribution, while ours does not require discretization, making it more precise. Furthermore, there are 11 different versions of TBFS which are based on 11 different classifier performance metrics. TBFS can also be extended to incorporate additional metrics.

The 11 threshold-based feature selection techniques are evaluated using software measurement data in our case study, including three data sets of release 3.0 of a real-world software project, Eclipse [13]. In order to evaluate the classification performance of the TBFS techniques on the smaller subsets of attributes, several classification models are built using five commonly used classifiers. Since related literature lacks general agreement on which performance metrics should be used for evaluating classification performance [9, 8], learners are evaluated using eight performance metrics. The experiments demonstrate that the choice of a performance metric can significantly influence the conclusions. In addition, we have found four distinct patterns when we use eight performance metrics to order 11 threshold-based feature selection techniques.

The main contribution of this work is the presentation of a set of novel threshold-based feature selection techniques and an assessment and comparison of these feature selection methods using eight performance metrics and five commonly used classifiers.

The remainder of the paper is organized as follows. Section 2 explains our threshold-based feature selection methodology. Section 3 describes the learners, performance

Algorithm 1: Threshold-based Feature Selection Algorithm

input :

1. Data set D with features $F^j, j = 1, \dots, m$;
2. Each instance $x \in D$ is assigned to one of two classes $c(x) \in \{fp, nfp\}$;
3. The value of attribute F^j for instance x is denoted $F^j(x)$;
4. Threshold-based feature ranking technique $\omega \in \{\text{BFM, OR, PO, PR, GI, MI, KS, DV, BGM, AUC, PRC}\}$;
5. A predefined threshold: number (or percentage) of the features to be selected.

output:

Selected feature subsets.

for $F^j, j = 1, \dots, m$ **do**

 Normalize $F^j \mapsto \hat{F}^j = \frac{F^j - \min(F^j)}{\max(F^j) - \min(F^j)}$;

 Calculate metric ω using attribute $\hat{F}^j, \omega_i(\hat{F}^j)$.

Create feature ranking \mathbb{R} using $\omega_i(\hat{F}^j) \forall j$.

Select features according to feature ranking \mathbb{R} and a predefined threshold.

metrics and case study data sets used in this work, and presents the experimental results. Finally, we conclude the paper in Section 4 and provide suggestions for future work.

2 Threshold-based Feature Selection Techniques

Filter-based feature ranking techniques (filters) rank features independently without involving any learning algorithm. Eleven threshold-based feature selection techniques (TBFS) were developed and implemented by our research group within Weka [12]. The procedure is shown in Algorithm 1. First each attribute's values are normalized between 0 and 1 by mapping F^j to \hat{F}^j . The normalized values are treated as posterior probabilities. Each independent attribute is then paired individually with the class attribute and the reduced two attribute data set is evaluated using 11 different performance metrics based on a set of posterior probabilities. In standard binary classification, the predicted class is assigned using the default decision threshold of 0.5. The default decision threshold is often not optimal, especially when the class is imbalanced. Therefore, we propose the use of performance metrics which allow for finding the optimal threshold.

The true positive (TPR), true negative (TNR), false positive (FPR), false negative (FNR), precision (PRE), negative predicted value (NPV) [11] rates can be calculated at each threshold $t \in [0, 1]$ relative to the normalized attribute \hat{F}^j . The threshold-based attribute ranking techniques we propose utilize these rates as described below.

- **Best F-measure (BFM):** is a single value metric derived from the F-measure that originated from the field of

information retrieval.

$$\text{BFM} = \max_{t \in [0,1]} \frac{(1 + \beta^2) \times TPR(t) \times PRE(t)}{\beta^2 \times TPR(t) + PRE(t)}.$$

β is set to 1 in this study. The maximum F-measure (BFM) is obtained when varying the decision threshold value between 0 and 1.

- **Odds Ratio (OR):** is the maximum value of the ratio of the product of correct (true positive rate times true negative rate) to incorrect (false positive rate times false negative rate) predictions. The odds ratio is defined as:

$$\text{OR} = \max_{t \in [0,1]} \left(\frac{TPR(t)}{FPR(t)} \right) \left(\frac{TNR(t)}{FNR(t)} \right)$$

- **Power (PO):** is a measure that avoids common false positive cases while giving stronger preference for positive cases [5]. Power is defined as:

$$\text{PO} = \max_{t \in [0,1]} ((TNR(t))^k - (FNR(t))^k)$$

where $k = 5$.

- **Probability Ratio (PR):** is the sample estimate probability of the feature given the positive class divided by the sample estimate probability of the feature given the negative class [5]. The probability ratio is defined as:

$$\text{PR} = \max_{t \in [0,1]} \frac{TPR(t)}{FPR(t)}$$

- **Gini Index (GI):** measures the impurity of a data set. GI for the attribute is then the minimum Gini index at all decision thresholds $t \in [0, 1]$.

$$\text{GI} = \min_{t \in [0,1]} [2PRE(t)(1 - PRE(t)) + 2NPV(t)(1 - NPV(t))].$$

- **Mutual Information (MI):** measures the mutual dependence of the two random variables. High mutual information indicates a large reduction in uncertainty, and zero mutual information between two random variables means the variables are independent.

- **Kolmogorov-Smirnov (KS):** utilizes the Kolmogorov-Smirnov statistic to measure the maximum difference between the empirical distribution function of the attribute values of instances in each class. The larger the distance between the distribution functions, the better the attribute is able to distinguish between the two classes. It is effectively the maximum difference between the curves generated by the true positive and false positive rates as the decision threshold changes from 0 and 1.

Table 1. Performance Metrics using NB

| Data | Filter | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM |
|----------------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| Eclipse 3.0-10 | BFM | 0.8936 | 0.4402 | 0.5144 | 0.5448 | 0.7431 | 0.8535 | 0.7668 | 0.8544 |
| | OR | 0.8606 | 0.3998 | 0.4900 | 0.5195 | 0.7203 | 0.8384 | 0.7496 | 0.8391 |
| | PO | 0.8966 | 0.4479 | 0.5168 | 0.5431 | 0.7334 | 0.8607 | 0.7603 | 0.8611 |
| | PR | 0.8408 | 0.3863 | 0.4803 | 0.5109 | 0.7178 | 0.8047 | 0.7472 | 0.8085 |
| | GI | 0.8439 | 0.3889 | 0.4804 | 0.5089 | 0.7151 | 0.8056 | 0.7452 | 0.8089 |
| | MI | 0.8715 | 0.4331 | 0.5101 | 0.5364 | 0.7342 | 0.8398 | 0.7603 | 0.8414 |
| | KS | 0.8713 | 0.4478 | 0.5118 | 0.5420 | 0.7330 | 0.8429 | 0.7596 | 0.8446 |
| | DV | 0.8986 | 0.4388 | 0.5214 | 0.5454 | 0.7453 | 0.8633 | 0.7689 | 0.8635 |
| | BGM | 0.8622 | 0.4412 | 0.5133 | 0.5466 | 0.7360 | 0.8365 | 0.7618 | 0.8384 |
| | AUC | 0.8988 | 0.4558 | 0.5336 | 0.5570 | 0.7536 | 0.8637 | 0.7755 | 0.8640 |
| PRC | 0.8936 | 0.4573 | 0.5203 | 0.5493 | 0.7395 | 0.8561 | 0.7647 | 0.8562 | |
| Eclipse 3.0-5 | BFM | 0.8863 | 0.6535 | 0.6495 | 0.6689 | 0.7670 | 0.8441 | 0.7846 | 0.8442 |
| | OR | 0.8830 | 0.6490 | 0.6412 | 0.6697 | 0.7633 | 0.8436 | 0.7812 | 0.8438 |
| | PO | 0.8885 | 0.6600 | 0.6527 | 0.6704 | 0.7666 | 0.8432 | 0.7848 | 0.8438 |
| | PR | 0.8810 | 0.6425 | 0.6336 | 0.6619 | 0.7613 | 0.8396 | 0.7789 | 0.8398 |
| | GI | 0.8813 | 0.6447 | 0.6312 | 0.6598 | 0.7598 | 0.8409 | 0.7776 | 0.8412 |
| | MI | 0.8845 | 0.6502 | 0.6502 | 0.6708 | 0.7671 | 0.8430 | 0.7848 | 0.8431 |
| | KS | 0.8862 | 0.6539 | 0.6469 | 0.6759 | 0.7631 | 0.8417 | 0.7817 | 0.8420 |
| | DV | 0.8856 | 0.6527 | 0.6555 | 0.6698 | 0.7687 | 0.8427 | 0.7865 | 0.8427 |
| | BGM | 0.8858 | 0.6532 | 0.6429 | 0.6746 | 0.7608 | 0.8427 | 0.7797 | 0.8431 |
| | AUC | 0.8847 | 0.6474 | 0.6484 | 0.6664 | 0.7653 | 0.8448 | 0.7834 | 0.8450 |
| PRC | 0.8851 | 0.6542 | 0.6547 | 0.6712 | 0.7671 | 0.8456 | 0.7853 | 0.8458 | |
| Eclipse 3.0-3 | BFM | 0.8129 | 0.6427 | 0.5645 | 0.6314 | 0.6594 | 0.7647 | 0.7034 | 0.7676 |
| | OR | 0.8091 | 0.6472 | 0.5790 | 0.6321 | 0.6777 | 0.7714 | 0.7136 | 0.7731 |
| | PO | 0.8163 | 0.6583 | 0.5854 | 0.6347 | 0.6792 | 0.7684 | 0.7162 | 0.7710 |
| | PR | 0.8107 | 0.6416 | 0.5793 | 0.6289 | 0.6804 | 0.7645 | 0.7144 | 0.7666 |
| | GI | 0.8108 | 0.6418 | 0.5800 | 0.6291 | 0.6809 | 0.7649 | 0.7148 | 0.7669 |
| | MI | 0.8124 | 0.6441 | 0.5625 | 0.6318 | 0.6582 | 0.7637 | 0.7024 | 0.7672 |
| | KS | 0.8109 | 0.6373 | 0.5595 | 0.6294 | 0.6536 | 0.7619 | 0.7002 | 0.7659 |
| | DV | 0.8140 | 0.6436 | 0.5643 | 0.6308 | 0.6585 | 0.7650 | 0.7031 | 0.7677 |
| | BGM | 0.8123 | 0.6420 | 0.5626 | 0.6306 | 0.6565 | 0.7632 | 0.7020 | 0.7663 |
| | AUC | 0.8101 | 0.6480 | 0.5819 | 0.6344 | 0.6770 | 0.7694 | 0.7143 | 0.7718 |
| PRC | 0.8106 | 0.6515 | 0.5878 | 0.6379 | 0.6814 | 0.7689 | 0.7177 | 0.7716 | |

Table 2. Performance Metrics using MLP

| Data | Filter | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM |
|----------------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| Eclipse 3.0-10 | BFM | 0.9034 | 0.5146 | 0.4143 | 0.5558 | 0.5534 | 0.8416 | 0.6510 | 0.8447 |
| | OR | 0.8817 | 0.4884 | 0.3994 | 0.5247 | 0.5395 | 0.8244 | 0.6428 | 0.8254 |
| | PO | 0.8982 | 0.5262 | 0.4333 | 0.5692 | 0.5692 | 0.8385 | 0.6596 | 0.8409 |
| | PR | 0.8528 | 0.4341 | 0.3556 | 0.4798 | 0.5003 | 0.7930 | 0.6222 | 0.7974 |
| | GI | 0.8512 | 0.4446 | 0.3531 | 0.4828 | 0.4957 | 0.7939 | 0.6202 | 0.7974 |
| | MI | 0.8922 | 0.4920 | 0.4044 | 0.5312 | 0.5410 | 0.8338 | 0.6444 | 0.8367 |
| | KS | 0.8962 | 0.5226 | 0.4467 | 0.5555 | 0.5785 | 0.8407 | 0.6648 | 0.8431 |
| | DV | 0.9030 | 0.5321 | 0.4574 | 0.5697 | 0.5866 | 0.8416 | 0.6699 | 0.8440 |
| | BGM | 0.8945 | 0.5182 | 0.4357 | 0.5563 | 0.5684 | 0.8393 | 0.6601 | 0.8414 |
| | AUC | 0.9097 | 0.5289 | 0.4526 | 0.5588 | 0.5861 | 0.8544 | 0.6681 | 0.8564 |
| PRC | 0.8981 | 0.5117 | 0.4293 | 0.5532 | 0.5662 | 0.8374 | 0.6572 | 0.8408 | |
| Eclipse 3.0-5 | BFM | 0.9183 | 0.7622 | 0.6306 | 0.6977 | 0.7202 | 0.8661 | 0.7536 | 0.8667 |
| | OR | 0.9178 | 0.7555 | 0.6256 | 0.6944 | 0.7172 | 0.8645 | 0.7511 | 0.8651 |
| | PO | 0.9226 | 0.7606 | 0.6310 | 0.6920 | 0.7196 | 0.8614 | 0.7534 | 0.8618 |
| | PR | 0.9147 | 0.7520 | 0.6310 | 0.6905 | 0.7213 | 0.8566 | 0.7543 | 0.8574 |
| | GI | 0.9147 | 0.7530 | 0.6337 | 0.6952 | 0.7235 | 0.8593 | 0.7559 | 0.8602 |
| | MI | 0.9162 | 0.7617 | 0.6286 | 0.7000 | 0.7187 | 0.8622 | 0.7525 | 0.8632 |
| | KS | 0.9194 | 0.7604 | 0.6248 | 0.6990 | 0.7193 | 0.8651 | 0.7522 | 0.8656 |
| | DV | 0.9217 | 0.7650 | 0.6219 | 0.6965 | 0.7122 | 0.8690 | 0.7477 | 0.8695 |
| | BGM | 0.9178 | 0.7594 | 0.6284 | 0.6982 | 0.7209 | 0.8649 | 0.7536 | 0.8654 |
| | AUC | 0.9213 | 0.7674 | 0.6340 | 0.6998 | 0.7241 | 0.8690 | 0.7563 | 0.8695 |
| PRC | 0.9221 | 0.7657 | 0.6269 | 0.6967 | 0.7180 | 0.8671 | 0.7517 | 0.8676 | |
| Eclipse 3.0-3 | BFM | 0.8778 | 0.7511 | 0.6073 | 0.6987 | 0.7027 | 0.8180 | 0.7323 | 0.8195 |
| | OR | 0.8742 | 0.7510 | 0.6225 | 0.6930 | 0.7098 | 0.8154 | 0.7408 | 0.8159 |
| | PO | 0.8848 | 0.7624 | 0.6313 | 0.7110 | 0.7146 | 0.8297 | 0.7443 | 0.8302 |
| | PR | 0.8796 | 0.7575 | 0.6325 | 0.6981 | 0.7228 | 0.8194 | 0.7483 | 0.8202 |
| | GI | 0.8793 | 0.7577 | 0.6323 | 0.6978 | 0.7227 | 0.8190 | 0.7482 | 0.8199 |
| | MI | 0.8827 | 0.7604 | 0.6354 | 0.7105 | 0.7209 | 0.8253 | 0.7476 | 0.8256 |
| | KS | 0.8857 | 0.7633 | 0.6346 | 0.7124 | 0.7222 | 0.8254 | 0.7482 | 0.8261 |
| | DV | 0.8780 | 0.7512 | 0.6134 | 0.6992 | 0.7079 | 0.8182 | 0.7360 | 0.8189 |
| | BGM | 0.8862 | 0.7657 | 0.6359 | 0.7133 | 0.7230 | 0.8278 | 0.7487 | 0.8284 |
| | AUC | 0.8835 | 0.7596 | 0.6260 | 0.7087 | 0.7108 | 0.8293 | 0.7414 | 0.8296 |
| PRC | 0.8850 | 0.7622 | 0.6335 | 0.7106 | 0.7179 | 0.8297 | 0.7463 | 0.8300 | |

- *Deviance (DV)*: is the minimum residual sum of squares based on a threshold t . That is, it measures the sum of the squared errors from the mean class given a partitioning of the space based on the threshold t .
- *Best Geometric Mean (BGM)*: is a single-value performance measure that ranges from 0 to 1 which is calculated by finding the maximum geometric mean of TPR and TNR as the decision threshold is varied between 0 and 1:

$$BGM = \max_{t \in [0,1]} \sqrt{TPR(t) \times TNR(t)} \quad (1)$$

- *Area Under ROC (Receiver Operating Characteristic) Curve (AUC)*: has been widely used to measure classification model performance [4]. AUC is a single-value measurement that ranges from 0 to 1. The ROC curve is used to characterize the trade-off between true positive rate and false positive rate. In this study, ROC curves are generated by varying the decision threshold t used to transform the normalized attribute values into a predicted class.
- *Area Under the Precision-Recall Curve (PRC)*: is a single-value measure that originated from the area of information retrieval. The area under the PRC ranges from 0 to 1. The PRC diagram depicts the trade off between recall and precision.

In this study, AUC, PRC, BFM, and BGM serve as both aids to the feature ranking process and the final inductive algorithm evaluation process (see Section 3.2).

3 Experiments

3.1 Classifiers

Classifiers are built with five well-known classification algorithms [12] including naïve Bayes (NB), multilayer perceptron (MLP), k -nearest neighbors (KNN), support vector machine (SVM) [3] and logistic regression (LR). These were selected because of their common use in data mining applications. Unless stated otherwise, the default parameter settings are used for the learners as specified in Weka [12]. Parameter settings were changed only when a significant improvement in performance based on preliminary experimentation was obtained. For the KNN classifier, 5 neighbors were used and the *distanceWeighting* parameter was set to “Weight by 1/distance”. For the MLP learner, *hiddenLayers* was changed to 3 to define a network with one hidden layer containing three nodes, and *validationSetSize* was changed to 10 to cause the classifier to leave 10% of the training data aside to be used as a validation set to determine when to stop the iterative training process. For SVM, the complexity constant c was changed from 1.0 to 5.0 and *buildLogisticModels* was enabled.

3.2 Classifier Performance Metrics

Eight performance metrics are used in the study including AUC, PRC, DFM (Default F-measure corresponds to a decision threshold value of 0.5), BFM (Best F-Measure which is the largest value of F-measure when varying the decision threshold value between 0 and 1), DGM (Default Geometric Mean), BGM (Best Geometric Mean), DAM

Table 3. Performance Metrics using KNN

| Data | Filter | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM |
|----------------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| Eclipse 3.0-10 | BFM | 0.9125 | 0.4544 | 0.4138 | 0.5176 | 0.5699 | 0.8600 | 0.6569 | 0.8616 |
| | OR | 0.8935 | 0.4485 | 0.3630 | 0.4743 | 0.5237 | 0.8446 | 0.6316 | 0.8451 |
| | PO | 0.9206 | 0.4668 | 0.4010 | 0.5318 | 0.5607 | 0.8724 | 0.6518 | 0.8736 |
| | PR | 0.8653 | 0.3797 | 0.3077 | 0.4014 | 0.4644 | 0.8145 | 0.6030 | 0.8166 |
| | GI | 0.8683 | 0.3955 | 0.3360 | 0.4094 | 0.4889 | 0.8131 | 0.6153 | 0.8162 |
| | MI | 0.8993 | 0.4484 | 0.4049 | 0.4982 | 0.5620 | 0.8458 | 0.6532 | 0.8466 |
| | KS | 0.9004 | 0.4614 | 0.4030 | 0.5128 | 0.5614 | 0.8498 | 0.6519 | 0.8505 |
| | DV | 0.9165 | 0.4631 | 0.3951 | 0.5211 | 0.5558 | 0.8635 | 0.6493 | 0.8651 |
| | BGM | 0.8955 | 0.4546 | 0.4029 | 0.5056 | 0.5578 | 0.8425 | 0.6500 | 0.8430 |
| | AUC | 0.9193 | 0.4825 | 0.4055 | 0.5110 | 0.5613 | 0.8695 | 0.6523 | 0.8702 |
| PRC | 0.9206 | 0.4672 | 0.4241 | 0.5076 | 0.5853 | 0.8715 | 0.6656 | 0.8728 | |
| Eclipse 3.0-5 | BFM | 0.9229 | 0.7456 | 0.6312 | 0.6728 | 0.7353 | 0.8482 | 0.7620 | 0.8494 |
| | OR | 0.9180 | 0.7229 | 0.6211 | 0.6681 | 0.7253 | 0.8436 | 0.7549 | 0.8450 |
| | PO | 0.9202 | 0.7391 | 0.6267 | 0.6654 | 0.7321 | 0.8445 | 0.7597 | 0.8457 |
| | PR | 0.9157 | 0.7214 | 0.6147 | 0.6613 | 0.7222 | 0.8377 | 0.7520 | 0.8387 |
| | GI | 0.9161 | 0.7235 | 0.6146 | 0.6620 | 0.7227 | 0.8387 | 0.7522 | 0.8402 |
| | MI | 0.9223 | 0.7431 | 0.6519 | 0.6755 | 0.7489 | 0.8454 | 0.7731 | 0.8471 |
| | KS | 0.9221 | 0.7374 | 0.6488 | 0.6771 | 0.7509 | 0.8448 | 0.7740 | 0.8461 |
| | DV | 0.9240 | 0.7452 | 0.6336 | 0.6746 | 0.7351 | 0.8512 | 0.7623 | 0.8525 |
| | BGM | 0.9246 | 0.7460 | 0.6524 | 0.6852 | 0.7516 | 0.8493 | 0.7749 | 0.8513 |
| | AUC | 0.9235 | 0.7421 | 0.6490 | 0.6773 | 0.7448 | 0.8494 | 0.7702 | 0.8508 |
| PRC | 0.9224 | 0.7357 | 0.6250 | 0.6713 | 0.7330 | 0.8484 | 0.7599 | 0.8493 | |
| Eclipse 3.0-3 | BFM | 0.8889 | 0.7368 | 0.6481 | 0.6854 | 0.7440 | 0.8101 | 0.7611 | 0.8108 |
| | OR | 0.8851 | 0.7262 | 0.6539 | 0.6899 | 0.7459 | 0.8118 | 0.7638 | 0.8125 |
| | PO | 0.8981 | 0.7521 | 0.6717 | 0.7145 | 0.7624 | 0.8263 | 0.7766 | 0.8271 |
| | PR | 0.8847 | 0.7183 | 0.6466 | 0.6826 | 0.7429 | 0.8117 | 0.7603 | 0.8124 |
| | GI | 0.8845 | 0.7183 | 0.6466 | 0.6820 | 0.7429 | 0.8110 | 0.7603 | 0.8118 |
| | MI | 0.8898 | 0.7402 | 0.6515 | 0.6944 | 0.7451 | 0.8164 | 0.7626 | 0.8170 |
| | KS | 0.8921 | 0.7495 | 0.6501 | 0.7025 | 0.7440 | 0.8206 | 0.7617 | 0.8214 |
| | DV | 0.8915 | 0.7377 | 0.6515 | 0.6912 | 0.7466 | 0.8164 | 0.7633 | 0.8169 |
| | BGM | 0.8930 | 0.7508 | 0.6571 | 0.7072 | 0.7506 | 0.8238 | 0.7668 | 0.8244 |
| | AUC | 0.8951 | 0.7562 | 0.6645 | 0.7009 | 0.7535 | 0.8190 | 0.7701 | 0.8197 |
| PRC | 0.8974 | 0.7516 | 0.6709 | 0.7100 | 0.7610 | 0.8248 | 0.7757 | 0.8257 | |

Table 4. Performance Metrics using LR

| Data | Filter | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM |
|----------------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| Eclipse 3.0-10 | BFM | 0.9127 | 0.5661 | 0.4838 | 0.6060 | 0.6241 | 0.8616 | 0.6908 | 0.8623 |
| | OR | 0.8745 | 0.5025 | 0.4041 | 0.5416 | 0.5628 | 0.8326 | 0.6531 | 0.8341 |
| | PO | 0.9106 | 0.5679 | 0.4740 | 0.6062 | 0.6138 | 0.8611 | 0.6849 | 0.8621 |
| | PR | 0.8705 | 0.4422 | 0.3819 | 0.4778 | 0.5485 | 0.8237 | 0.6448 | 0.8252 |
| | GI | 0.8687 | 0.4486 | 0.3833 | 0.4839 | 0.5470 | 0.8257 | 0.6441 | 0.8268 |
| | MI | 0.9047 | 0.5407 | 0.4686 | 0.5687 | 0.6087 | 0.8527 | 0.6814 | 0.8531 |
| | KS | 0.9050 | 0.5617 | 0.4741 | 0.5728 | 0.6098 | 0.8575 | 0.6818 | 0.8593 |
| | DV | 0.9159 | 0.5659 | 0.4742 | 0.5981 | 0.6125 | 0.8651 | 0.6840 | 0.8658 |
| | BGM | 0.9045 | 0.5605 | 0.4882 | 0.5801 | 0.6230 | 0.8525 | 0.6902 | 0.8545 |
| | AUC | 0.9097 | 0.5617 | 0.4724 | 0.5677 | 0.6045 | 0.8604 | 0.6788 | 0.8607 |
| PRC | 0.9072 | 0.5502 | 0.4650 | 0.5796 | 0.5997 | 0.8589 | 0.6762 | 0.8595 | |
| Eclipse 3.0-5 | BFM | 0.9406 | 0.7952 | 0.6697 | 0.7297 | 0.7564 | 0.8854 | 0.7800 | 0.8860 |
| | OR | 0.9446 | 0.7968 | 0.6768 | 0.7299 | 0.7638 | 0.8874 | 0.7857 | 0.8879 |
| | PO | 0.9375 | 0.7891 | 0.6423 | 0.7192 | 0.7367 | 0.8817 | 0.7644 | 0.8818 |
| | PR | 0.9379 | 0.7918 | 0.6765 | 0.7273 | 0.7642 | 0.8821 | 0.7859 | 0.8827 |
| | GI | 0.9372 | 0.7912 | 0.6780 | 0.7316 | 0.7660 | 0.8809 | 0.7873 | 0.8814 |
| | MI | 0.9383 | 0.7971 | 0.6636 | 0.7227 | 0.7516 | 0.8859 | 0.7762 | 0.8860 |
| | KS | 0.9349 | 0.7907 | 0.6579 | 0.7141 | 0.7479 | 0.8824 | 0.7733 | 0.8827 |
| | DV | 0.9411 | 0.7944 | 0.6671 | 0.7251 | 0.7544 | 0.8837 | 0.7784 | 0.8841 |
| | BGM | 0.9376 | 0.7963 | 0.6600 | 0.7201 | 0.7483 | 0.8832 | 0.7738 | 0.8837 |
| | AUC | 0.9394 | 0.7905 | 0.6685 | 0.7303 | 0.7577 | 0.8872 | 0.7807 | 0.8875 |
| PRC | 0.9421 | 0.7911 | 0.6686 | 0.7227 | 0.7577 | 0.8853 | 0.7807 | 0.8857 | |
| Eclipse 3.0-3 | BFM | 0.9097 | 0.7822 | 0.6361 | 0.7314 | 0.7182 | 0.8479 | 0.7461 | 0.8480 |
| | OR | 0.9061 | 0.7816 | 0.6440 | 0.7243 | 0.7235 | 0.8408 | 0.7506 | 0.8409 |
| | PO | 0.9095 | 0.7863 | 0.6437 | 0.7288 | 0.7224 | 0.8471 | 0.7500 | 0.8472 |
| | PR | 0.9053 | 0.7868 | 0.6561 | 0.7238 | 0.7348 | 0.8410 | 0.7588 | 0.8413 |
| | GI | 0.9054 | 0.7869 | 0.6566 | 0.7241 | 0.7352 | 0.8408 | 0.7591 | 0.8411 |
| | MI | 0.9076 | 0.7807 | 0.6382 | 0.7270 | 0.7186 | 0.8412 | 0.7469 | 0.8412 |
| | KS | 0.9077 | 0.7805 | 0.6356 | 0.7263 | 0.7164 | 0.8445 | 0.7453 | 0.8446 |
| | DV | 0.9115 | 0.7830 | 0.6368 | 0.7335 | 0.7191 | 0.8478 | 0.7467 | 0.8479 |
| | BGM | 0.9092 | 0.7821 | 0.6382 | 0.7260 | 0.7188 | 0.8456 | 0.7470 | 0.8457 |
| | AUC | 0.9089 | 0.7828 | 0.6456 | 0.7294 | 0.7258 | 0.8477 | 0.7520 | 0.8478 |
| PRC | 0.9088 | 0.7826 | 0.6472 | 0.7344 | 0.7273 | 0.8509 | 0.7531 | 0.8510 | |

(Default Arithmetic Mean), and BAM (Best Arithmetic Mean). The arithmetic mean uses the arithmetic mean of the true positive rate and true negative rate.

Note that the metrics used to measure the performance of the classifiers is completely independent from the metrics in the TBFS algorithm. For example, AUC is used both to select the most predictive subset of features using TBFS and AUC is also used to evaluate the classifiers constructed using this set of features. However the AUC-based TBFS technique can also be evaluated using other classifier performance metrics such as BAM or DGM.

3.3 Data Sets

Experiments conducted in this study use software metrics and defect data collected from release 3.0 of a real-world software project, the Eclipse project [13]. We transform the original data by: (1) removing all nonnumeric attributes, including the package names, and (2) converting the post-release defects attribute to a binary class attribute, fault-prone (fp) and not fault-prone (nfp). Membership in each class is determined by a post-release defects threshold λ , which separates fp from nfp packages by classifying packages with λ or more post-release defects as fp and the remaining as nfp. We chose three post-release defects thresholds $\lambda \in \{10, 5, 3\}$ to determine the defective instances. The derived data sets contain 208 attributes and 661 instances. We use these thresholds to obtain three different levels of class imbalance for Eclipse data sets. The proportions of fp modules of the three data sets are 6.2%, 14.83% and 23.75%.

3.4 Experimental Results and Analysis

In the experiments, ten runs of five-fold cross-validation are performed. For each of the five folds, one fold is used as test data while the other four are used as the training data. First, we rank the attributes using the 11 threshold-based feature ranking techniques separately. Once the attributes are ranked, the top $\lceil \log_2 208 \rceil = 8$ (there are 208 independent features) attributes are selected (as well as the class attribute) to yield final training data. Selecting eight attributes was deemed reasonable for these experiments, and space considerations keep us from presenting results with other parameter choices. This final training data is then used to build the classification model, the resulting model is applied to the test-fold, and the eight performance metrics are calculated.

The classification models are evaluated in terms of the eight performance metrics separately. All the results are reported in Table 1 through Table 4 (the detailed results for SVM are omitted for space considerations). The classifier performance metrics are provided in the columns, and the individual TBFS filters are listed as rows. Again note that AUC is listed both as a filter and performance metric, but the context should be clear given the explanations provided above. Each value presented in the table is the average over the ten runs of five-fold cross-validation outcomes. The best model for each data set is indicated in **boldfaced** print. Filter performance varies depending on both the learner and the performance metric. Table 5 presents the number of times each filter performed best relative to each performance metric, summarized across all five classifiers and three data sets together. No particular TBFS filter domi-

Table 5. Summary of Optimal TBFS Filter

| Filter | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM | Total | % of Total |
|--------|-----|-----|-----|-----|-----|-----|-----|-----|-------|------------|
| BFM | 0 | 1 | 1 | 0 | 2 | 2 | 1 | 2 | 8 | 6.7% |
| OR | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 2 | 5 | 4.2% |
| PO | 7 | 3 | 1 | 4 | 1 | 4 | 1 | 4 | 25 | 20.8% |
| PR | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0% |
| GI | 0 | 1 | 2 | 1 | 3 | 0 | 3 | 0 | 10 | 8.3% |
| MI | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 3 | 2.5% |
| KS | 0 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 2 | 1.7% |
| DV | 2 | 1 | 2 | 1 | 2 | 2 | 2 | 2 | 14 | 11.7% |
| BGM | 2 | 3 | 4 | 2 | 3 | 0 | 3 | 0 | 17 | 14.2% |
| AUC | 3 | 4 | 2 | 1 | 2 | 4 | 2 | 4 | 22 | 18.3% |
| PRC | 0 | 1 | 2 | 3 | 2 | 2 | 2 | 2 | 14 | 11.7% |

nates the others, but generally speaking, we can conclude that PO and AUC are most often the best technique, while PR, KS, MI and OR are rarely optimal.

A two-way ANOVA [1] was performed for each of the eight performance metrics separately. The two factors are Factor A, in which eleven threshold-based rankers were considered, and Factor B, in which five classifiers were included. In this ANOVA test, the results from all three data sets were taken into account together. A significance level of $\alpha = 5\%$ was used for all statistical tests. The ANOVA results are presented in Table 6. Focusing on Factor A, the test results indicate that for each performance metric, there was a significant difference between the average values of the 11 TBFS methods. For all eight performance metrics, the p -value is less than 5%, although the significance varies substantially among metrics (e.g., PRC in Table 6(b) compared to AUC in Table 6(a)). Multiple comparison tests were conducted on Factor A, since this study mainly focuses on the attribute selection techniques and their classifier performance evaluation. Both ANOVA and multiple comparison tests are implemented in MATLAB. An exhaustive discussion of Factor B is avoided due to space consideration.

The performance of the threshold-based filters was ranked from best to worst for each performance metric as shown in Table 7. Each filter is labeled with a superscript. The filters labeled with the same superscripts implies that they were from same performance group, in which no statistically significant difference was found between filters. Some findings can be summarized from Table 7: (1) Four distinct groups of results were found when we order 11 filters based on eight performance metrics (over all the classifiers built): (a) AUC, BAM, and BGM; (b) PRC; (c) BFM; and (d) DFM, DAM, and DGM. (2) Among the 11 threshold-based feature selection techniques, the performance of AUC-based filter performed best overall. PR- and GI-based filters performed worst, followed by OR regardless of performance metrics. While PO was most often the optimal technique (Table 5), this is somewhat offset by relatively worse performance in other situations.

Table 8 presents performances of the defect classification models built with the complete set of features. Comparing these results to Tables 1 through 4, classification models

Table 6. Analysis of Variance

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|--------|------------|
| A | 0.09 | 10 | 0.009 | 11.9 | 0 |
| B | 0.9073 | 4 | 0.2268 | 300.00 | 0 |
| Error | 1.2362 | 1635 | 0.0008 | | |
| Total | 2.2336 | 1649 | | | |

(a) AUC

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|-------|------------|
| A | 0.2857 | 10 | 0.0286 | 1.85 | 0.0481 |
| B | 3.901 | 4 | 0.9753 | 63.11 | 0 |
| Error | 25.2659 | 1635 | 0.0155 | | |
| Total | 29.4527 | 1649 | | | |

(b) PRC

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|------|------------|
| A | 0.2075 | 10 | 0.0208 | 2.06 | 0.0249 |
| B | 0.1645 | 4 | 0.0411 | 4.08 | 0.0027 |
| Error | 16.4901 | 1635 | 0.01009 | | |
| Total | 16.8621 | 1649 | | | |

(c) DFM

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|-------|------------|
| A | 0.2642 | 10 | 0.0264 | 4.14 | 0 |
| B | 0.9797 | 4 | 0.2449 | 38.38 | 0 |
| Error | 10.4327 | 1635 | 0.0064 | | |
| Total | 11.6766 | 1649 | | | |

(d) BFM

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|-------|------------|
| A | 0.1263 | 10 | 0.0126 | 2.18 | 0.0165 |
| B | 0.4417 | 4 | 0.1104 | 19.09 | 0 |
| Error | 9.458 | 1635 | 0.0058 | | |
| Total | 10.026 | 1649 | | | |

(e) DGM

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|--------|------------|
| A | 0.0908 | 10 | 0.0091 | 10.61 | 0 |
| B | 0.5093 | 4 | 0.1273 | 148.73 | 0 |
| Error | 1.3997 | 1635 | 0.0009 | | |
| Total | 1.9998 | 1649 | | | |

(f) BGM

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|-------|------------|
| A | 0.0453 | 10 | 0.0045 | 1.95 | 0.0348 |
| B | 0.1497 | 4 | 0.0374 | 16.13 | 0 |
| Error | 3.7929 | 1635 | 0.0023 | | |
| Total | 3.9879 | 1649 | | | |

(g) DAM

| Source | Sum Sq. | d.f. | Mean Sq. | F | p -value |
|--------|---------|------|----------|--------|------------|
| A | 0.0847 | 10 | 0.0085 | 10.54 | 0 |
| B | 0.4847 | 4 | 0.1212 | 150.76 | 0 |
| Error | 1.3141 | 1635 | 0.0008 | | |
| Total | 1.8835 | 1649 | | | |

(h) BAM

Table 7. Rank of Filters (Factor A)

| Metric | Rank of TBFS Filters (best → worst) | | | | | | | | | | |
|--------|-------------------------------------|-------------------|-------------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|------------------|-----------------|
| | AUC ^a | DV ^{ab} | PRC ^{ab} | PO ^{ab} | BFM ^{abc} | MI ^{bcd} | KS ^{bcd} | BGM ^{cd} | OR ^d | GI ^e | PR ^e |
| AUC | AUC ^a | DV ^{ab} | PRC ^{ab} | PO ^{ab} | BFM ^{abc} | MI ^{bcd} | KS ^{bcd} | BGM ^{cd} | OR ^d | GI ^e | PR ^e |
| PRC | AUC ^a | PRC ^a | PO ^a | DV ^a | KS ^a | BFM ^a | BGM ^a | MI ^{ab} | OR ^{abc} | GI ^{bc} | PR ^c |
| DFM | AUC ^a | BGM ^{ab} | PRC ^{ab} | BFM ^{ab} | DV ^{ab} | KS ^{ab} | PO ^{ab} | MI ^{abc} | OR ^{bcd} | GI ^{cd} | PR ^d |
| BFM | PO ^a | PRC ^{ab} | DV ^{ab} | AUC ^{ab} | BFM ^{ab} | BGM ^{ab} | KS ^{ab} | MI ^{ab} | OR ^{bc} | GI ^c | PR ^c |
| DGM | AUC ^a | BGM ^{ab} | PRC ^{ab} | BFM ^{ab} | DV ^{ab} | PO ^{ab} | MI ^{ab} | KS ^{ab} | OR ^{bc} | GI ^c | PR ^c |
| BGM | AUC ^a | PRC ^a | PO ^{ab} | DV ^{ab} | BFM ^{abc} | MI ^{bcd} | BGM ^{cd} | OR ^d | GI ^e | PR ^e | |
| DAM | AUC ^a | BGM ^{ab} | PRC ^{ab} | BFM ^{ab} | DV ^{ab} | PO ^{abc} | MI ^{abc} | KS ^{abc} | OR ^{bcd} | GI ^{cd} | PR ^d |
| BAM | AUC ^a | PRC ^a | PO ^{ab} | DV ^{abc} | BFM ^{abc} | KS ^{abc} | MI ^{bcd} | BGM ^{cd} | OR ^d | GI ^e | PR ^e |

Table 8. Performance of Full Data Sets

| Data | Learner | AUC | PRC | DFM | BFM | DGM | BGM | DAM | BAM |
|----------------|---------|--------|--------|--------|--------|--------|--------|--------|--------|
| Eclipse 3.0-10 | NB | 0.8685 | 0.3304 | 0.4710 | 0.4868 | 0.7666 | 0.8228 | 0.7811 | 0.8238 |
| | MLP | 0.7697 | 0.3836 | 0.4000 | 0.4539 | 0.5772 | 0.7435 | 0.6598 | 0.7526 |
| | KNN | 0.7325 | 0.3565 | 0.1959 | 0.4203 | 0.3364 | 0.7322 | 0.5556 | 0.7388 |
| | SVM | 0.8030 | 0.4067 | 0.4169 | 0.4506 | 0.6172 | 0.7680 | 0.6809 | 0.7697 |
| Eclipse 3.0-5 | LR | 0.6596 | 0.1993 | 0.2995 | 0.3355 | 0.5935 | 0.6600 | 0.6527 | 0.6764 |
| | NB | 0.8648 | 0.5113 | 0.5707 | 0.5934 | 0.7274 | 0.8104 | 0.7485 | 0.8111 |
| | MLP | 0.8422 | 0.6065 | 0.5750 | 0.6113 | 0.7072 | 0.8042 | 0.7383 | 0.8069 |
| | KNN | 0.8114 | 0.5880 | 0.5156 | 0.5828 | 0.6239 | 0.7694 | 0.6869 | 0.7729 |
| Eclipse 3.0-3 | SVM | 0.8897 | 0.6741 | 0.6150 | 0.6489 | 0.7498 | 0.8369 | 0.7691 | 0.8373 |
| | LR | 0.7632 | 0.4294 | 0.4974 | 0.5208 | 0.7016 | 0.7348 | 0.7198 | 0.7388 |
| | NB | 0.8119 | 0.5684 | 0.5475 | 0.6025 | 0.6617 | 0.7426 | 0.6972 | 0.7471 |
| | MLP | 0.8076 | 0.6408 | 0.5640 | 0.6102 | 0.6776 | 0.7483 | 0.7091 | 0.7534 |
| Eclipse 3.0-3 | KNN | 0.7770 | 0.5828 | 0.5016 | 0.5546 | 0.6299 | 0.7201 | 0.6711 | 0.7218 |
| | SVM | 0.8673 | 0.7216 | 0.6385 | 0.6667 | 0.7364 | 0.7953 | 0.7548 | 0.7959 |
| | LR | 0.7452 | 0.4984 | 0.5245 | 0.5431 | 0.6804 | 0.6960 | 0.6909 | 0.7035 |

built using smaller subsets of attributes selected with TBFS had better performances than those built with a complete set of attributes.

4 Conclusion

Numerous feature selection techniques have been proposed in the data mining and machine learning domains. The aim of feature selection is to remove irrelevant and redundant features with the primary objective of improving classifier performance. In this study, we present our newly proposed threshold-based feature selection techniques and compare their performance to classifiers constructed without the use of feature selection. Three data sets from a real-world software project were used, with different levels of class imbalance. Classification models were constructed using five commonly used methodologies and are evaluated using eight performance metrics. Threshold-based feature selection using the AUC parameter was shown to provide generally good performance, though the optimal filter often varied depending on the classifier, dataset, and performance metric. OR-, GI-, and PR-based filters in particular did not perform as well as the other filters. Furthermore, we have found four distinct patterns when utilizing eight performance metrics to order 11 threshold-based feature selection techniques. A final inference is that even after removing 96% of the available software metrics, the classification models were not adversely affected; in fact, in 95% of the cases the results were better.

Future work will involve conducting additional empirical studies with data from other software projects and application domains. Additional experiments should also be

conducted to analyze the impact of the number of selected features.

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