

## STATISTICAL PROPERTIES OF COMPOSITE DISTORTIONS IN HFC SYSTEMS AND THEIR EFFECTS ON DIGITAL CHANNELS

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### ABSTRACT

*The statistical properties of Composite Triple Beat (CTB) and Composite Second Order (CSO) distortion terms associated with the analog channels carried on Hybrid Fiber Coax (HFC) are presented. Both simulation and measurement results show that such distortion components falling on individual channels have amplitude Probability Density Function that is nearly Rayleigh distributed (having a Standard Deviation of 5.7 dB). It is shown that both CTB and CSO components have peak envelope power fluctuations that exceed their average (measured) power levels by more than 15 dB. The temporal statistical properties of these distortion components demonstrate peak envelope power fluctuations with characteristic times on the order of 100 microseconds. The implications for 256 QAM digital downstream channels on which such CTB and CSO components fall are discussed. It is shown that some currently prevailing link budget design practices leave margins for reliable 256 QAM operation wanting. This deficiency appears particularly in systems that are rich with Narrowcast combining of digital channels such as cable modem and Video on Demand (VOD) applications. Several mitigation strategies and improved design practices are suggested. These involve physical layer choices for deeper digital interleavers, establishing downstream QAM frequency offset relative to the analog channel grid, improving CTB and CSO specifications for cable modems and digital set-top tuners and adopting tighter aggregate noise floor specifications for head-end RF transmission gear.*

### 1 Introduction

Nonlinear distortions and limited dynamic range in multichannel carrier systems has received renewed attention with the proliferation of digital devices and the industry's move to launch 256 QAM digital services. Now, composite distortion components often become the bottleneck that never was for the predominant 64 QAM service. Although the installed base of digital subscriber set-tops and cable modems is predominantly 256 QAM capable, many cable operators have yet to migrate to 256 QAM transmissions successfully. As it turns out, the 256 QAM's whopping 44% increase in channel information payload capacity over that of 64 QAM comes at a considerable cost in noise and interference margin requirements. Operating reliable 256 QAM downstream links is more challenging due to the factors described in Section 5. Suffice it to say here that as a result of the cumulative effect of these factors, the noise margin left for further noise degradations in 256 QAM all but disappears [1].

### 2 Composite Distortions Effect on Digital Channels

Composite Triple Beats (CTB) and Composite Second Order (CSO) distortion components produced by intermodulation of analog TV carriers can become the dominant degrading factor for digital cable QAM channels [1],[2],[3],[4],[5]. It is generally accepted that in thermal noise environments, a Carrier to Noise Ratio ( $C/N$ ) of 30-35 dB provides adequate operating margins for 256 QAM [6]. It is also generally known that cable systems normally operate with CTB or CSO levels that meet or exceed a Carrier-to-Interference ( $C/I$ )

ratio of 53 dB, as required in Reference [6]. These levels correspond to a  $C/I$  of 47 dB for a QAM signal carried with levels that are 6 dB below the analog carriers. The question that may arise is *why should distortion components having average power levels that are 12-15 dB below the noise level have any appreciable degradation effects on the QAM channel performance?* The short answer is that the average envelope power of composite distortion terms (which is what one observes in a spectrum analyzer measurement) is deceptively low in comparison to its occasional peak envelope power.

### 3 Description of Composite Distortion Terms

In a multicarrier CATV system one often represents the signal to be communicated as

$$(1) \quad S(t) = \sum_{n=1}^N A_n \cos(\omega_n t + \theta_n),$$

where  $A_n$ ,  $\omega_n$  and  $\theta_n$  are the amplitude, the angular frequency and phase of the  $n^{\text{th}}$  carrier signal. We shall have occasion to investigate the unmodulated case,  $A_n = A$  for all  $n$  and the modulated case, where the modulations in  $A_n$  are sufficiently slow compared to the essential RF period of  $S(t)$  so as to treat them as constants (or as random variables) during such RF period discussed below. This assumption is justified since statistically, the baseband video modulation power spectrum has negligible energy at 6 MHz or 1.25 MHz, which are possible nominal periodicities of the RF signal. Furthermore, for television signals, we shall assume that other subcarriers such as the single sided audio and chroma subcarriers associated with each television carrier are sufficiently low in amplitude in comparison with the visual carrier so as to treat them as a separate additive noise process. The above assumptions permit us to treat Equation (1) as a reasonable representation of the dominant signal in our problem.

Upon subjecting  $S(t)$  to a memoryless nonlinear distortion device having a transfer function given by  $y = x + \alpha x^2 + \beta x^3$ , where  $x$  is the input voltage and  $y$  the output voltage, we obtain intermodulation products of second and third order and in this work we have assumed no higher order distortion exist in the nonlinear transfer function. The type and relative amplitudes of the intermodulation components that are so obtained are well known and are tabulated elsewhere [7]. We shall be interested in components of the following form:

(1-A) Second-Order

$$\frac{1}{2} \alpha A_n A_k \cos[(\omega_n \pm \omega_k)t + \theta_n \pm \theta_k]$$

(1-B) Third-Order

$$\frac{1}{4} \beta A_n A_k A_m \cos[(\omega_n \pm \omega_k \pm \omega_m)t + \theta_n \pm \theta_k \pm \theta_m]$$

Channel frequency plans in which virtually all carriers are nominally 6 MHz apart result in accumulation of many distortion components falling on the same nominal frequency. The manner by which these terms combine and the amplitude excursions of the resultant composite waveform falling on each channel depend on several factors. These factors are the number of carriers  $N$ , the specific arrangement of the amplitudes, the frequencies and the phases ( $A_n$ ,  $\omega_n$  and  $\theta_n$ ). It is important to note that even in the simplest case in which no modulation is assumed (i.e.  $A_n = A$  for all  $n$ ), a particular choice of the remaining parameters  $\omega_n$  and  $\theta_n$  may result in a solution that will not generally apply to any other combination. Furthermore, the actual values of these parameters may never be known for any particular head-end. With tens of frequencies involved, identifying any frequency combinations that may yield coherent combining (for which  $\omega_p = \omega_n \pm \omega_k \pm \omega_m$ , for example) would be of

particular significance but intractable. Moreover, if the whole set of channels is made coherent by locking to a comb generator for Incrementally Related Carriers (IRC) or Harmonically Related Carriers (HRC), than one would need to specify only each of the phase values  $\theta_n$  and the result will be specific to that phase constellation but not necessarily to any other<sup>1</sup>. Thus, it becomes clear that countless combinations would have to be considered as special cases and that the utility of information pertaining to any specific combination for making general statements is doubtful at best.

An alternative approach we adopt here is to make the (realistic and inevitable) assumption that all the frequencies  $\omega_n$  are linearly independent over the rational field. Stated another way, we assume that there exists no set of  $N$  integers  $Q_n$ 's (positive, zero or negative) such that

$$\sum_{n=1}^N Q_n \omega_n = 0.$$

It is only under such an assumption (see footnote 3), that one may obtain results that apply across many different frequency realizations within the tolerance of the nominal frequency plan. For each such realization (a given collection of  $\omega_n$  and  $\theta_n$ ) in our model, an *unmodulated* signal  $S(t)$  of Equation (1) is deterministic and nothing about it is random. Because the precise frequencies are assumed to be linearly independent, the period of the signal  $S(t)$  is infinite. Consequently, the period of any of its distortion components is also infinite. With this assumption, it is mathematically possible to show that a characterization of *any* feature, measure, rate of occurrence, or distribution over a long enough observation period  $T$  from

<sup>1</sup> In fact, there are very atypical (but deliberate) phase constellations that yield very low distortion values that are otherwise extremely unlikely to be found at random. A method for arriving at such constellations is described in [8].

$t_0$  to  $t_0+T$ , would be repeatable regardless of the value  $t_0$ . In contrast, this cannot be assured for choices of exact frequencies that are linearly dependent over the rational field. We note that, strictly speaking, the *nominal* frequencies of the Standard CATV channel plan are a linearly dependent set of frequency values. However, in non-coherent headends, their *actual* values are given by<sup>2</sup>

$$(2) \quad \begin{aligned} \omega_n &= (n+8) \cdot \omega_c + \omega_0 + \Delta\omega_n \\ &= 2\pi [(n+8)f_c + f_0 + \Delta f_n] \end{aligned}$$

where  $f_c = 6$  MHz,  $f_0 = 1.25$  MHz (the visual carrier offset from the channel edge) and  $\Delta f_n$  is the individual actual deviation from the nominal frequency due to tolerance. These deviations can be on the order of a few hundred Hz to a few kHz, and are the basis and justification for the assumption we make about their linear independence over the rational field<sup>3</sup>. When one uses the values in Equation (2) for the frequencies, one obtains composite distortion frequencies that have linear combinations of the deviation values. For example, third order components falling on frequencies  $\omega_n + \omega_k - \omega_m$  have frequency values of  $p\omega_c + \omega_0 + \Delta\omega_n + \Delta\omega_k - \Delta\omega_m$  with  $p$  an integer designating the channel. Similarly second order terms falling on frequencies  $\omega_n + \omega_k$  have frequency values of

<sup>2</sup> We are ignoring the special case of Channels 5 and 6 that are offset by 2 MHz. Throughout this study, these channels and all others up to and including A4 were omitted, i.e.  $A_n=0$  for  $n=4$  through  $n=9$  in Equations (1) and (2) above. The last channel in the array was at  $n=81$ , making up a total of 75 carriers.

<sup>3</sup> Because there is no relationship among the deviations  $\Delta f_n$  of channels in a non-coherent system, these offset values can be regarded as real numbers near 0, drawn at random. Because the rationals form a set of measure-zero on the real line, the probability that any random pair of real numbers  $\Delta f_n$  and  $\Delta f_k$  are linearly dependent over the rationals (i.e. that  $\Delta f_n / \Delta f_k$  is rational) is zero. In other words, the probability that this model does *not* apply to a cable system having a non-coherent standard frequency plan is *zero*.

$q\omega_c + 2\omega_0 + \Delta\omega_n + \Delta\omega_k$  with  $q$  being another channel designating integer. Because the deviation frequencies  $\Delta\omega_n$  are linearly independent over the rationals for all values of  $n$ , we conclude that *all possible beat frequencies produced by any combination of such deviation terms must all be distinct frequencies.*

The observation above provides certain clarity and resolution to predictions of the average power levels of composite distortion terms, as there are no terms that can combine coherently. In this case, counting the number of composite terms on any given frequency range would yield the exact power level of such components. Thus, precise derivations for such numbers [9] or tight approximations [10] can be very useful and the theoretical prediction of the average power in the unmodulated case is therefore straightforward. It is other characteristics of the composite distortion terms such as the envelope fluctuations and their temporal behavior that are of great interest. To that end, this author has embarked on a theoretical study comprising an analytical effort [11] and an empirical simulation effort, parts of which are reported in the next sections.

#### 4 Mathematical Background and the Simulation Approach

By rewriting (1) using the defined frequencies of (2) we find that the simulation problem at hand is that of forming representations of, and operations with,  $S(t)$  given by:

$$(3) \quad S(t) = \sum_{n=1}^N A_n \cos \{ [(n+8)\omega_c + \omega_0]t + \Delta\omega_n t + \theta_n \}$$

wherein we have grouped separately the frequency terms that correspond to the (linearly dependent) nominal frequencies. One approach for studying the distortion components would be to select the frequencies and apply the expression for  $S(t)$  from (3) into

the nonlinear transfer function  $y = x + \alpha x^2 + \beta x^3$  by setting  $x = S(t)$ . Processing the results to obtain a representative measure by an average over the observation time interval would be required. If, for example, we wish to study a composite second order frequency-addition beat of the form given in (1-A), we would have a collection of like-frequency terms that fall on the sum-frequency of interest designated by the frequency index  $p$ , giving rise to a signal proportional to:

$$(3-A) \quad \begin{aligned} y_{CSO}(p) &= \\ &= \sum_n A_n A_{p-n} \cos[(\omega_n + \omega_{p-n})t + \theta_n + \theta_{p-n}] = \\ &= \sum_n A_n A_{p-n} \cos[(p\omega_c + 2\omega_0 + \Delta\omega_n + \Delta\omega_{p-n})t + \theta_n + \theta_{p-n}] \end{aligned}$$

These terms form a narrow band signal about the frequency  $p\omega_c + 2\omega_0$  with an envelope function given by

$$(3-B) \quad \begin{aligned} \text{Env}[y_{CSO}(p), (t)] &= \\ &= \sum_n \sum_m A_n A_{p-n} A_m A_{p-m} \times \\ &\times \cos[(\Delta\omega_n + \Delta\omega_{p-n} - \Delta\omega_m - \Delta\omega_{p-m})t + \\ &\quad + \theta_n + \theta_{p-n} - \theta_m - \theta_{p-m}] \end{aligned}$$

where the meaning of a signal's envelope is that ascribed to it in the classic treatise by Dugundji [12]. In this work we are focusing on the statistical characteristics of the envelope (amplitudes) of these composite distortion terms rather than their instantaneous RF statistics because it is more closely related to the demodulated baseband disturbances that affect BER performance of digital set-tops and cable modems. When we analyze such envelope terms, we obtain functions that depend on the carriers' amplitudes, their deviation frequencies and phases  $\Delta\omega_n, \theta_n$ , but not explicitly on their actual frequencies. Thus, for a given signal  $S(t)$  and a given set of amplitudes, forming a statistical measure over time associated with such envelope terms

essentially amounts to time-averaging of some (nonlinear) function  $F_S(\Delta\omega_n t, \theta_n; n=1 \text{ to } N)$ . The function  $F_S(\bullet)$  might be a histogram of sorts or the envelope value occurrence rate, or joint correlation products of envelope values, etc. Thus, the function  $F_S(\bullet)$  is representative of the kind of processing, data collection and classification that would be used. Fortunately, the assumption that the frequencies of  $S(t)$  are linearly independent provides a powerful tool to simplify the simulations of these time-averages, regardless of the form of  $F_S(\bullet)$ . It is based on a fundamental theorem in Ergodic Theory known as the *Kronecker-Weyl* theorem [13]:

#### 4.1 The Kronecker-Weyl Theorem.

Let the function  $F(\psi_1, \psi_2, \dots, \psi_N) \equiv F(\Psi)$  be a multiply periodic function defined on the  $N$ -dimensional torus  $0 \leq \psi_j < 2\pi, j=1, 2, \dots, N$  such that  $F(\Psi') = F(\Psi'')$  if  $\psi'_j = \psi''_j$  (modulo  $2\pi$ ) for all  $j$ . The *Kronecker-Weyl* (K-W) theorem states the following:

If  $\theta_j, j=1, 2, \dots, N$  are constants and if

$$(4) \quad \psi_j = \Omega_j t + \theta_j \text{ for all } j,$$

wherein the frequencies  $\Omega_j, j=1, 2, \dots, N$  are linearly independent over the rational field, than

$$(5) \quad \frac{1}{T} \int_0^T F[\psi_1(t), \psi_2(t), \dots, \psi_N(t)] dt \xrightarrow{T \rightarrow \infty} \int_0^{2\pi} \dots \int_0^{2\pi} \frac{F(\psi_1, \psi_2, \dots, \psi_N)}{(2\pi)^N} d\psi_1 d\psi_2 \dots d\psi_N$$

Stated another way, under the conditions that satisfy the K-W theorem, one can avoid having to select the frequency deviations  $\Delta\omega_j$  for averaging over long time periods and replace time averages by averages over all the phases. For example, the CSO envelope term

expressed above is simulated by identifying  $\Omega_j$  of the K-W theorem with  $\Delta\omega_j$  and by using (4) and rewriting (3) as:

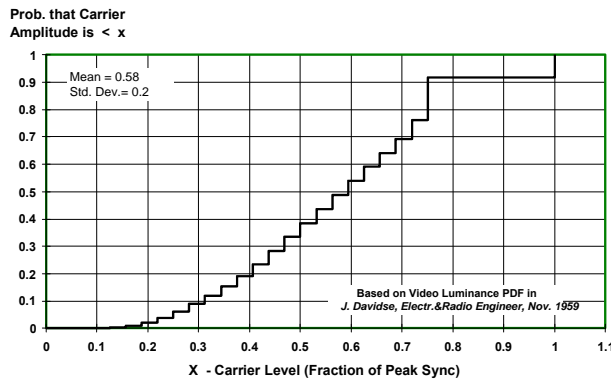
$$(6) \quad S(t) = \sum_{n=1}^N A_n \cos \{ [(n+8)\omega_c + \omega_0] t + \psi_n \}$$

This approach also applies for CTB or other distortion terms. In our computer simulations we thus form an ensemble of uniformly distributed random phase vectors  $\Psi \equiv (\psi_1, \psi_2, \dots, \psi_N)$  with independent components on the  $N$  dimensional torus. For each such randomly drawn phase vector we compute  $S(t)$  in accordance with Equation (6) and obtain a function of  $t$  that becomes a member of the analysis ensemble. Since we selected the Standard frequency plan, the period of every  $S(t)$  of the ensemble is 1.25 MHz and after appropriate model distortions are introduced, an FFT routine is employed to obtain envelopes of composite distortion terms on specific frequencies. It should be noted that the dependence on time remaining in  $S(t)$  in (6) is used only to obtain the Fourier spectral components of interest, and not for time averaging.

#### 4.2 Modulation Statistics

In addition to simulations of the CW case, we simulated independent modulations on each of the carriers. Because in these simulations, we were focused only on first-order statistics (i.e. amplitude distributions and joint densities), time correlation effects (i.e. second-order statistics) associated with the analog video signals were not needed and only first order statistics of the amplitudes were used. These distributions were computationally constructed from first-order statistics of NTSC luminance values, as they control the amplitude of the visual carrier. NTSC Luminance distribution values were taken from the work done by Philips researchers [14] in their work that led to the PAL system.

Appropriate account was made for blanking (75% level) and synch (100% level) periods and the resultant distribution is shown in Figure 1. Effects of amplitude modulation were simulated by forming the ensemble of functions of Equation (6) by the expanded ensemble of random variables, comprising  $\{\psi_1, \psi_2, \dots, \psi_N, A_1, A_2, \dots, A_N\}$ , where the phases  $\psi_j$  are drawn independently from a uniform distribution over  $[0, 2\pi]$  and the amplitudes  $A_j$  are drawn independently from the distribution in Figure 1. In that fashion, millions of realizations of  $S(t)$ , and consequently all related CSO and CTB distortion terms on every channel, were computed and analyzed as an ensemble. The results for the modulated and the unmodulated cases are shown in subsequent sections.



**Figure 1.** Cumulative probability distribution of RF amplitudes of video modulated NTSC television signal. This function was used for simulating the independent modulation of 75 carriers. The function was constructed based on video luminance distributions provided in Reference [14].

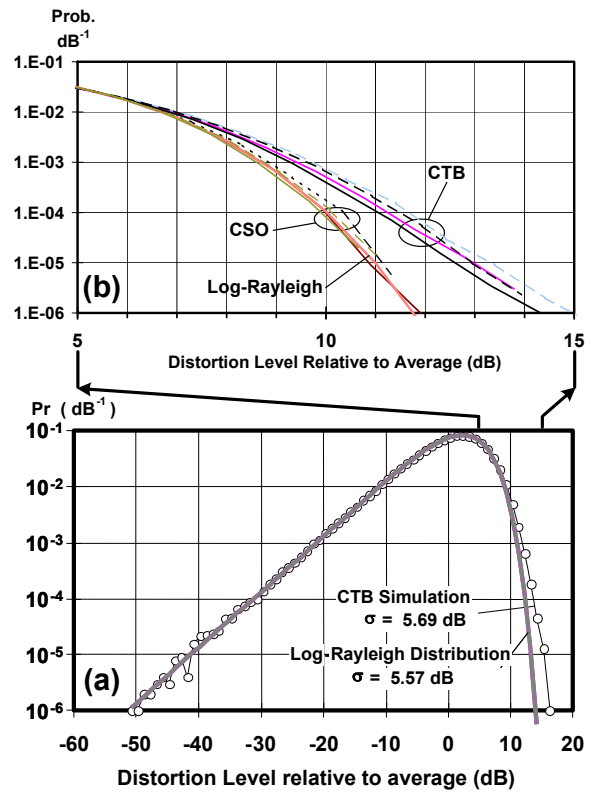
### 4.3 Composite Distortions – Simulation Results and Discussion

#### 4.3.1 Amplitude Statistics of Composite Distortions

This author encountered only a paucity of studies related to the probability density functions of CTB/CSO distortion components. One histogram was reported for CW HRC system [15], although it was not clear what the source of phase fluctuation was. A more comprehensive landmark study involving real

head-end in a controlled laboratory was reported in [4]. Both our simulations and the above referenced measurement results show that these distortion components falling on individual channels have amplitude Probability Density Functions (PDF) that are nearly Rayleigh. The Rayleigh probability density function is given by [16]:

$$f(x) = \frac{x}{a^2} \exp\left(-\frac{x^2}{2a^2}\right)$$



**Figure 2.** Probability density function of the amplitude of simulated CTB and CSO terms due to third order and second order distortions in a CATV system using the Standard Frequency plan with 75 analog video modulated carriers. On the ordinate, the amplitude squared is expressed in dB relative to the average envelope value and the corresponding probability per dB is plotted in the co-ordinate. For comparison, a Rayleigh density transformed to the dB scale (thus called Log-Rayleigh) is also shown in solid line. An expanded view from 5 to 15 dB is provided in (b), where curves for the CW case and the modulated case are shown with solid lines and broken lines respectively.

Figure 2a shows the simulation results for the probability density function of the amplitude of a simulated CTB term due to third order distortion in a CATV system employing the Standard Frequency plan with 75 analog video modulated carriers. For comparison, a Rayleigh density transformed to the dB scale (thus called Log-Rayleigh) is also shown. The Rayleigh density is relevant in this comparison because it describes the envelope probability density of a Gaussian process, which is the limit case for a linear combination of a large number of arbitrarily distributed, statistically independent random processes. One would expect that because the CTB and CSO terms encountered in CATV are comprised respectively from thousands and hundreds of beat components, the Rayleigh limit would be nearly approached. However, while there appears to be a good match at lower amplitude levels, deviations from the Rayleigh curve at large relative amplitudes are seen for CTB in Figure 2b. This slight deviation is likely due to the statistical dependence among these thousands of components. It is argued that, in this case, because there are only  $2 \times 75 = 150$  independent degrees of freedom (random phase and amplitude of each of the 75 carriers) affecting the phase and amplitude values of the individual *thousands* of beat components, these must be statistically dependent. Because the number of components in the CSO term is of the order of less than 100, these component values depend less on common degrees of freedom and are less correlated. The degree and differences of the correlations for CSO and CTB terms and their respective effects on envelope statistics are further addressed in [11].

It is noteworthy that examination of distortion terms on different channels reveals that, whereas the absolute levels of the envelopes differ, the PDFs of the CTB and CSO components on every channel essentially follow closely the results for the CTB term

shown in Figure 2(a) if they are normalized to their respective average envelope power. Moreover, each of these distributions, like the Rayleigh distribution, has a variance that is proportional to its mean. When used on a 'dB relative to average' scale, this means that the standard deviation  $\sigma$  in dB is constant. For the Log-Rayleigh case, it can be shown that  $\sigma = 5.7$  dB and we note that the results for CSO/CTB (as seen in Figure 2) terms do not differ appreciably from this value. However, at the tail of the distribution, CTB peak values are slightly higher than those of the CSO and Log-Rayleigh terms (Figure 2b). In that figure, the modulated case (broken lines) is seen to have higher relative envelope values than the CW case for the same probabilities, with a difference of less than half a dB at the level of interest. Although the absolute values for the modulated case are some 2.5 dB lower than the CW case (having peak sync amplitudes), we are showing here the results normalized to average power.

The trends observed in these simulations are fairly consistent with measurement results of a real headend as reported in [4] (see Figures 8 and 9 in that reference), although the differences between the modulated case and the CW case in the measurement results seem to be slightly larger. It is conjectured that because the video sources in that system were received from a satellite feed, as would be the case for many cable systems, some channels were in fact correlated, as they carry program material that is frame synchronized across various channels<sup>4</sup>. Hence, more of the variations attributable to amplitude modulation were based on even fewer degrees of freedom, increasing the relative statistical dependence among these components.

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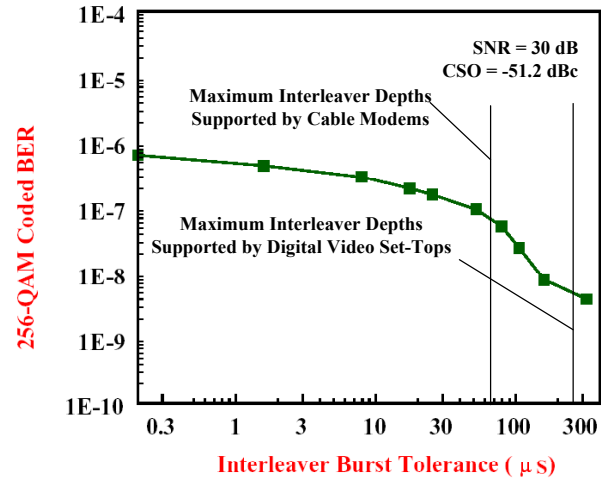
<sup>4</sup> Many of the services such as the HBO group of channels come from a single uplink facility wherein the practice of video 'house sync' is used. Other examples of groups that are likewise synchronized are the Viacom feeds and the USA Network feeds.

Turning back to the question raised at the outset, tying these statistics to the impact on digital channels is now rather straightforward. As Figure 2b shows, both CTB and CSO components have significant likelihood of having peak envelope power fluctuations that exceed their average power levels by more than 12-18 dB. Unfortunately, when such fluctuations occur in a composite distortion term having an *average* level of  $-47$  dBc, levels up to  $-29$  dBc can be experienced. Thus, even in situations in which the prevailing noise floors are rather intuitively low, significant occasional impairments can still be observed. To relate these results to 256 QAM Bit Error Rates (BER) and consequential video impairments, we turn next to the temporal characteristics of these composite distortion components.

### 4.3.2 Time Domain Statistics of Composite Distortions

Although we have not simulated the second-order properties of these distortion components, several observations can be made. When high envelope fluctuations of composite distortion terms occur, bursts of bit errors can be generated on the 256 QAM link. Degradations due to bursts that are relatively short can be mitigated in part by the interleaving used on the digital link. Such interleaving is part of the Forward Error Correction (FEC) system used in QAM transmission. Clearly, the severity of the degradations would be higher for burst errors having durations that exceed the interleaver depth capability. Figure 3 shows experimental results that demonstrate this trend for 256 QAM. This figure shows substantial reduction in coded error rate with interleavers having storage depths longer than 50-100 microseconds. Improvements start to level-off at above 300  $\mu$ s, indicating that burst events that are longer than 200  $\mu$ s are more rare. Note that the highest slope in improvement indicates the most likely duration. Thus, this observation shows that the characteristic

duration of CSO peak envelope fluctuations is on the order of 100  $\mu$ s. These results appear consistent with other studies on CSO/CTB distortion effects. See for example the similar average durations (60  $\mu$ s) reported by Germanov [2].



**Figure 3.** Coded bit error rate of 256 QAM link perturbed by CSO distortion as a function of interleaver burst span. Source of BER results: Ovardia [3].

Whereas both authors in References [2] and [3] report this characteristic duration time, neither suggests a mechanism, a reason or a cause for the observed 60-100  $\mu$ s characteristic times. As explained below, these characteristic times are simply related to the *correlation times* of the individual composite distortion components. These, in turn, are inversely related to the effective bandwidth occupied by such distortion components.

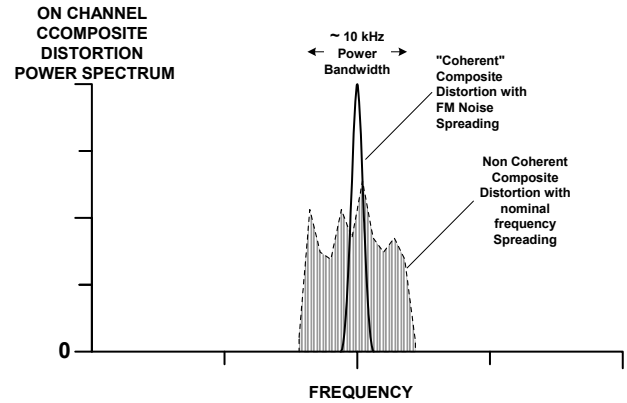
Figure 4 depicts a conceptual rendition of the power spectrum of a composite distortion term produced in a non-coherent frequency plan. Because most of the power in these distortion terms is distributed around frequencies that are a linear combination of the nominal frequencies of the contributing carriers (i.e.,  $f_1 \pm f_2 \pm f_3$ , for CTB, or  $f_1 \pm f_2$  for CSO), the spectral spreading for most of the energy will

be on the order of twice or three times the *frequency tolerance* of all transmitters. Some energy due to video modulation in the first (dominant 15.7 kHz horizontal rate) sidebands will widen this somewhat to a power bandwidth on the order of 10 kHz. For such narrow-band processes, the correlation times are approximately inversely proportional to the power bandwidth  $\Delta f$  and for a 10 kHz wide CTB or CSO spectral “clump”, one obtains a characteristic time of  $\tau = 1/\Delta f = 1/10^4 = 100\mu s$ . Due to such temporal correlations, the envelope value cannot change appreciably in less than 50-100  $\mu s$ , thereby giving rise to peaks having such durations. Ironically, modern (and more frequency-accurate) transmitters wherein all distortion terms fall nearly on the same frequency, the effective power bandwidth could be substantially smaller (as shown schematically in Figure 4). This will result in longer characteristic times for burst errors associated with composite distortions.

Unfortunately, as shown in Figure 3, cable modems under DOCSIS are designed with insufficient interleaver depth to adequately protect against the *most likely* burst durations, as they are limited to a protection depth of 66  $\mu s$  in the 256 QAM mode. In contrast, that same memory limit provides for a longer (95 $\mu s$ ) interleaver span in the 64 QAM mode, which further enhances the error tolerance of 64 QAM links compared to 256 QAM. Most digital video set-tops operating in 256 QAM cannot protect fully against CSO/CTB burst errors as their maximum interleaver depth is marginal at 264  $\mu s$ .

It is in the context of this CTB/CSO burst vulnerability of 256 QAM, that we examine the effect of additive noise in the channel. Importantly, Figure 3 shows that a *C/N* value of 30 dB, a value that some would judge as sufficiently safe, has a dramatically inadequate *coded* error rate performance for

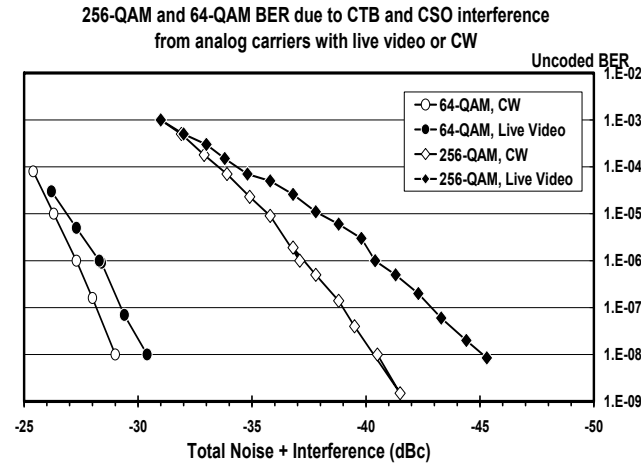
256 QAM operation under CSO distortion values that actually meet most MSO’s operating standards.



**Figure 4.** Conceptual rendition of the power spectrum of a composite distortion term produced in a non-coherent frequency plan and that produced in a coherent plan, wherein all distortion terms fall on the same frequency. Because most of the power is distributed around frequencies  $f_1 \pm f_2 \pm f_3$  (for CTB) or  $f_1 \pm f_2$  (for CSO), the spectral spreading for most of the energy will be on the order of several times the frequency tolerance of all transmitters. Some energy due to video modulation in the first 15.7 kHz (horizontal rate) sidebands will widen this somewhat to a power bandwidth on the order of 10 kHz.

Figure 5 shows measurement results reported in [4] using real set-tops and real head-end live video sources to modulate each channel in the analog tier. Uncoded bit error rates were recorded as a function of total interference and noise power. Note that at target BER values of  $10^{-8}$ , up to an additional 15 dB (!) of Noise+Interference margin is required for 256 QAM over that of 64 QAM. This increment is significantly larger than the 5.6 dB theoretical increment expected in pure random noise channels [17]. It is clearly related to the stacking of unfavorable parameters used in 256 QAM as enumerated in Section 5. Consequently, as further elaborated below and in reference to the results shown in Figure 5, this author suggests that under CSO/CTB average power levels that are within current operational CATV specifications, a 40 dB  $C/(N+I)$ , corresponding to a 256 QAM BER of  $10^{-6}$ , would *not* provide adequate margin

for reliable 256 QAM operation and that rather,  $C/(N+I)$  values in the range of 43-45 dB (approaching uncoded BER of  $10^{-8}$ ) would be required for a Quasi-Error-Free (QEF) 256 QAM operation<sup>5</sup>.



**Figure 5.** The measured effect of composite distortions on uncoded BER of 256 QAM link as compared with 64 QAM. CTB and CSO distortions were from analog carriers that were either modulated (Live Video) or unmodulated (CW). Note that at target BER values of  $10^{-8}$ , an additional 11 dB of Noise+Interference margin is required for 256 QAM over that of 64 QAM. Source: Stoneback et al. [4].

Finally, it should be appreciated that the frequencies of many digital 256 QAM channels are likely to be situated above the 550 MHz boundary and, as such, will be subject to both CTB and CSO. In this case, two distortion contributions should be accounted for. For our purposes below, we assume two composite distortion components each at a level of  $-55$  dBc. This corresponds to  $-49$  dBc with respect to the 256 QAM

signal, resulting in an average composite distortion level of  $-46$  dBc.

### 4.3.3 How large can CSO/CTB envelope fluctuations become?

The answer to this question depends on the observation interval. For practical purposes, we first present an intuitive approach to this problem in order to clarify the reasons for a substantial rethinking of the required margins for reliable 256 QAM operation.

We pose the question slightly differently by noting that the problem is essentially that of Level Crossing Rate. Next, we note that according to the discussion above, the envelope of the composite distortion term is essentially uncorrelated with its values separated by more than the characteristic time. Thus, for approximation purposes, we assume that one requires time separations of more than  $300 \mu\text{s}$  in order that the values of the envelope at these times be essentially statistically independent. This means that on average, every  $300 \mu\text{s}$  the envelope has an independent opportunity to achieve the range of values in accordance with the probability density shown in Figure 2. Stated another way, every  $300 \mu\text{s}$ , there is an independent experiment drawing at random a new envelope value with *a-priori* probability shown in Figure 2. If one uses the North American QEF rate as the permissible error event rate, then on average, one has 15 minutes of multiple  $300 \mu\text{s}$  long experiments to encounter one error event. We assuming for simplicity that the average distortion level is at such a level that only the highest excursion causes an uncorrected error. This means that we have  $15 \times 60 / (300 \times 10^{-6}) = 3 \cdot 10^6$  independent experiments, of which only one produces the largest envelope value causing an error event. Stated another way, the level crossing probability need only be one in  $3 \cdot 10^6$  (i.e.,  $3.33 \times 10^{-7}$ ) to reach the QEF limit. By inspecting Figure 2b for CTB and roughly

<sup>5</sup> Quasi Error Free (QEF) reception is more stringent than, and should be distinguished from, reception at the impairment Threshold Of Visibility (TOV). The Europeans set the QEF standard for DVB at levels achieving less than one uncorrected error event per hour [18]. In North America, J-83 Annex B defines QEF at less than one uncorrected error event per 15 minutes [21],[22]. The latter uncorrected error event rate corresponds to a BER =  $4.0\text{E-}11$  at the input of the MPEG-2 demultiplexer.

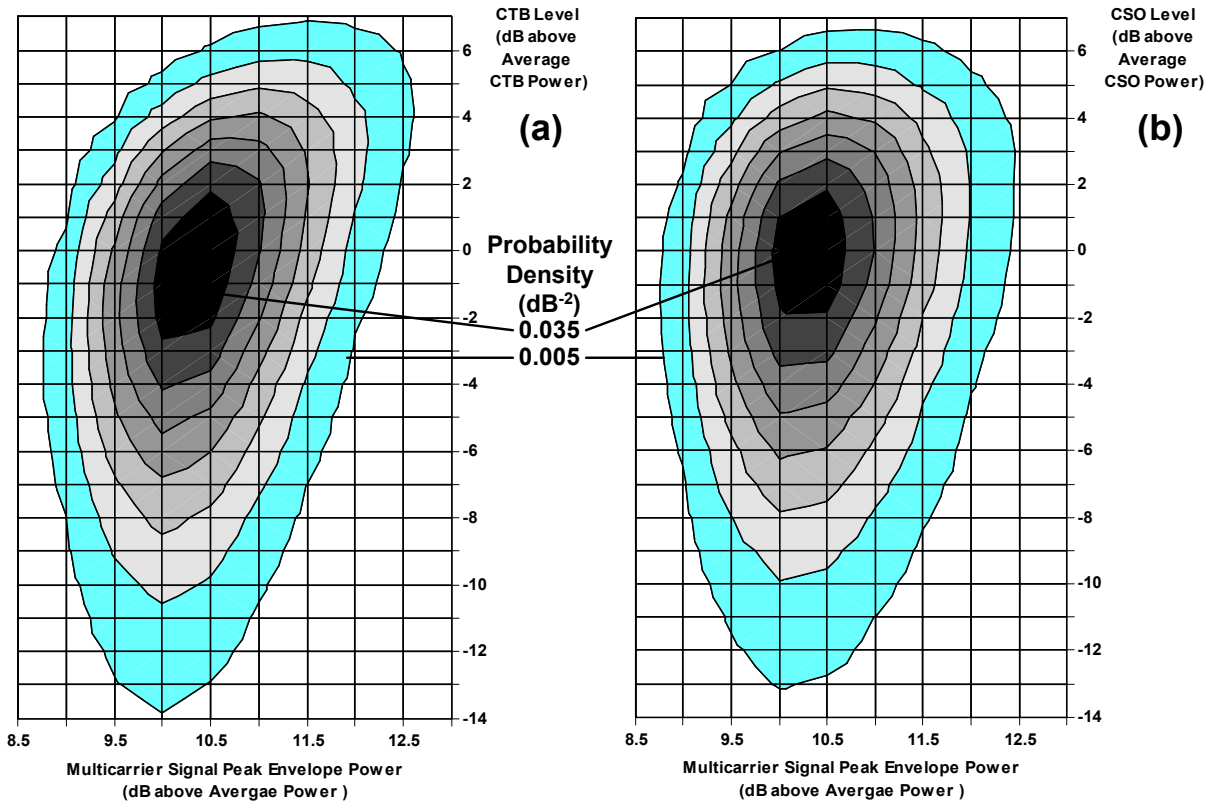
extrapolating down below the  $10^{-6}$  probability density line, one can estimate that by integrating its tail over the last few dB bins, we would pick up a probability mass of  $3.33 \times 10^{-7}$  for all values above 16 dB. This way, we estimated that the probability that the envelope exceeds the value of 16 dB is  $3.33 \times 10^{-7}$ . This means that the CTB envelope will exceed a level that is 16 dB above its mean at an average rate of once per 15 minutes – the QEF rate.

#### 4.3.4 CSO/CTB Relationship to peak amplitudes of multicarrier signals.

Over the years, an intuition and some folklore seemed to have developed among CATV engineers with respect to the causal relationship of composite distortion fluctuations and excessive amplitude excursions of the composite multicarrier signal. This intuitive view envisions situations in which occurrences of high peak amplitudes of the multicarrier signal are the cause of, and are therefore time-coincident with, interference transients associated with excessive distortion components. To some engineers, this view appears to be further supported by observations that a rapid increase in distortion-induced impairment rates are seen when nonlinear devices are driven beyond certain threshold levels. The intuitive theory related to that observation is that at those high signal levels, the composite amplitudes of the multicarrier signal reach clipping (saturation) levels, which *simultaneously* produces transient distortion products. Numerous measurements were attributed to such mechanism and several models based on this theory were published and analyzed (see [19] and the extensive reference list in [20]). As demonstrated below, peak amplitude fluctuations of CSO or CTB terms produced by *pure quadratic and 3<sup>rd</sup> order* nonlinear characteristics (without any clipping limits) can produce sharp degradation effects with increased drive levels that are often erroneously attributed to the

proverbial clipping mechanism at multicarrier signal levels that are well below actual clipping levels. To that end, simulation results for the Joint Probability Density of the envelope of a multicarrier signal and the envelope of resultant composite distortion components falling out of the analog channel tier (on channel 105), where digital signals might be carried are shown with contour plots in Figure 6. Note that very little correlation exists between the instantaneous levels of distortion terms and the composite signal. It is seen that the highest peak values of CTB (a) or CSO (b) will be encountered even when the composite multicarrier envelope itself is around its most likely value – well below its peak values. Although the CTB plot shows mild correlation at high levels, virtually all occurrences of large peak values for CSO and CTB are found with composite multicarrier amplitudes that are within 2 dB of their average.

In this regard, it is therefore clear that an ‘abrupt’ or sharp degradation can result by simply overdriving a *smooth* second-order or third-order nonlinearity. This can be readily seen in Figure 2, which shows that at the tail of the density function, where peak values can reach an observable degradation event, there is roughly one order of magnitude increase in occurrence rate for every dB increase of average distortion power. For CTB distortions, this means that if a drive level is just before the Threshold Of Visibility (TOV), overdriving the device by only one more dB, causes CTB levels to increase by 2 dBc, which corresponds to 100-fold (!) increase in the occurrence rate of visible degradations. At an initial TOV condition of, say, once every 10 seconds, the degradation rate would rise to 10 per second. That dramatic change in error event rate over a one dB level change would surely look like a “clipping” phenomenon to many folks...but it is not. It is simply the result of *overdriving* the nonlinear device over its *smooth* nonlinear range.



**Figure 6.** Simulation results for the Joint Probability Density of the envelope of a multicarrier signal with 75 carriers and the envelope of resultant composite distortion components on individual high channels. Note that very little correlation exists between the instantaneous levels of distortion terms and the composite signal. It is seen that the highest peak values of CTB (a) or CSO (b) will be encountered even when the composite multicarrier envelope is around its most likely value. In other words, “clipping” is not the most likely cause of CTB/CSO peak value excursions. Probability density contours are 0.005 per  $\text{dB}^2$  apart.

In fact, in some devices, clipping values would be far higher than the levels that would otherwise render *smooth* nonlinear devices inoperable due to overdrive. There is no doubt that in some situations, clipping is a factor in observed degradations. However, as we have seen, “clipping” is not the most likely cause of excessive CTB/CSO peak value excursions. By definition, it is the higher order distortion terms that must be associated with clipping. On this likelihood balance, perhaps a more fitting title for the article in [19] would have been “Don’t Get *Overdriven* on the Information Highway”....

## 5 Moving Forward with 256 QAM

### 5.1 Where we are

The previous sections illustrated how the challenges associated with operating a reliable 256 QAM service far exceed those associated with the 64 QAM digital service to which operators have grown accustomed. The reasons for the substantial difference in immunity from interference between the two formats can be found by examining their parameters. A summary of relevant factors is shown in Table 1.

Item	64 QAM	256 QAM	Comment on 256 QAM vs. 64 QAM
Constellation Density	8 x 8	16 x 16	
Half Symbol Specing to RMS Signal (dB)	-16.23	-22.30	6 dB denser
Nearest Symbol Angular Separation (Degrees)	7.7	3.7	Less than half
Symbol Rate (MSPS)	5.056941	5.360537	
Channel Data Rate (Mbps)	30.341646	42.884296	
Information bit rate (Mbps)	26.97035	38.8107	44% More Traffic
Overall Channel Utilization Rate	88.89%	90.50%	Due to Coding and Framing Overhead
Excess Bandwidth Roll-off Factor	0.18	0.12	Higher implementation loss with small Roll-off
Maximum Interleaver Span (µsec)	379	264	Most Set-Tops have this limitation.

**Table 1.** Comparison of various transmission parameters of 64 QAM and 256 QAM in the North American standard. See [21],[22].

These factors and others are addressed below:

- (a) Symbol constellation density is two times that of 64 QAM in each dimension. This means that relative to the signal level, decision regions in the 256 QAM signal space occupy an area that is one quarter of that of 64 QAM.
- (b) Burst error interleaver depth is limited in 256 QAM to 66 µs as opposed to 95 µs for 64 QAM in cable modems. In most set tops, the corresponding limitations are 264 µs and 380 µs respectively.
- (c) Coding Gain is lower for the 256 QAM format which has a trellis code rate of 19/20, dedicating one bit out of 20 for forward error correction versus one out of 15 bits used in the trellis code for 64 QAM.
- (d) Spectral Roll-Off Factor of 0.12 for 256 QAM (vs. 0.18 for 64 QAM) further reduces demodulator “eye opening” margin, which increases demodulation implementation losses.
- (e) Reduced Immunity to CSO and CTB distortion products (as discussed above).
- (f) Higher Susceptibility to phase noise [3] and ‘microphonics’. This factor can

easily account for a couple of dB of margin degradation.

- (g) Increased Tracking Time of the Adaptive Equalizer. Due the finer constellation of 256 QAM, channel adaptation time to sufficiently low symbol interference can take longer than in 64 QAM, especially if the demodulator employs a smaller step size for the coefficient updates in 256 QAM. A longer equalizer convergence time can degrade its ability to effectively track and null out a discrete interferer with level and spectral fluctuations at rates that exceed the equalizer convergence time constant<sup>6</sup>.

Operators cannot change these factors but they can take steps to improve the viability of 256 QAM in a growing number of systems.

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<sup>6</sup> Convergence times of the order of 2,000-10,000 symbols are not uncommon. This means that for a 5 MSPS QAM signal, fluctuations faster than 1 kHz would not be tracked well. Unfortunately, as seen above, the characteristic times of the CSO/CTB fluctuations are an order of magnitude faster. However, in the CW mode, these CSO and CTB components have a narrower spectral spreading and consequently might be better tracked by the equalizer. This may explain the data in Figure 5 showing the significant improved immunity of demodulators subject to CW CSO/CTB interference as compared to modulated CSO/CTB interference.

## 5.2 Where we need to go

In order to successfully employ 256 QAM services we would be well advised to consider the following mitigation measures and improved practices:

### 5.2.1 Control and improve CSO/CTB levels

This is an obvious item, but operators should consider reviewing their plant distortion budgets. A  $-53$  dBc average at the subscriber tap would not leave any margin for subscriber equipment degradations. In addition, CSO/CTB specifications of subscriber tuner distortion warrant further scrutiny. Several cable modem tuner suppliers offer specifications for CSO and CTB that are in the  $-50$  dBc range. As explained above, if such average levels of distortions are encountered ( $-44$  dBc for the digital signal), 256 QAM operation would be unreliable<sup>7</sup>

### 5.2.2 Judiciously choose proper channel frequency offsets

As described above, CSO and CTB components have most of their energy clustered in a spectral region spanning no more than 30 kHz. The most powerful CTB component consists of a combination of terms with frequencies  $2f_1-f_2$ , which fall on what would otherwise be the NTSC visual carrier frequency for that channel. Thus, it is narrowly concentrated 1.25 MHz above the channel edge. In a paper presented to the Joint EIA-NCTA Engineering Committee a decade ago [24], this author suggested the use of a frequency offset scheme that can virtually eliminate interference to digital channels from these CTB components by shifting the digital

channels block up by 1.25 MHz with respect to the analog channel boundaries. This way, the CTB components would be situated at the edge of (in between) the digital channels in the offset block, where there is considerable rejection by the receiver's SAW filter and the digital matched Nyquist filter. As discussed in [24], this relative offset is also optimal for minimizing subjective effects of third-order noise distortion emanating from the digital channels and falling on the analog channels.

Unfortunately, not all distortion terms are being rejected by this proposed scheme. Second order distortion terms of the  $f_1 + f_2$  class, situated 2.5 MHz above the channel edge, are not rejected. Since their level may increase at higher frequencies in the channel lineup (accompanied by a fortuitous decrease in the levels of CTB terms), one may wish to institute a new offset of an *additional* 1.25 MHz for digital channels above a certain cross-over frequency, where CTB levels are lower than CSO levels. Thus, proper channel offsets becomes a balancing act, since one cannot avoid both the CSO and CTB terms simultaneously. Fortunately for HRC system operators, both CSO and CTB terms fall on the same frequencies (the harmonics of 6 MHz), thereby making the 1.25 MHz relative offset a very effective mitigation tool. Thus, in these HRC analog channel lineup systems, digital channels would be best situated in conformance to the *Standard* channel plan and not the HRC plan.

### 5.2.3 Maintain QAM transmitter phase noise and head-end aggregate noise power at low levels.

In Reference [1], this author shows the significant impact of noise aggregation from many transmitter sources at the headend and hubs. It is shown that under currently prevailing headend and HFC signal transport practices, mass deployment of certain classes of QAM transmitters and upconverters used (or proposed to be used) for VOD, may not scale-up well because of excessive noise

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<sup>7</sup> For 256 QAM, the cable modem multicarrier loading test in the DOCSIS ATP [23] permits a test under which the total power of 30 dBmV is distributed across 5 carriers (one signal of interest, four other) not on image or adjacent channels. However, such test does not guarantee that any of the intermodulation components fall on the channel of interest. Furthermore, CSO and CTB from only 4 carriers produce much lower peak envelope power fluctuations than 80-channel source having the same total power.

accumulation from adjacent channel modulated distortion terms as well as from broadband noise. It is further shown in [1] that as operators expand and carry up to 50 digital channels on their downstream lineup, the use of lower performance QAM transmitters can result in a 2.4 dB C/(N+I) loss at the subscriber tap compared to the levels that can be realized with transmitters that meet the DOCSIS downstream QAM transmission requirements. These DOCSIS requirements are provided in Table 6-15 of its Radio Frequency Interface Specification [25]. Furthermore, QAM transmitter phase noise levels that have very little measurable effects on 64 QAM, may have significant degradation effects on 256 QAM links and thus it is also important to adopt DOCSIS' integrated phase noise specifications. These are found in the DOCSIS document referenced above. Finally, note that in adopting the RF DOCSIS requirements for head-end QAM modulators and upconverters, cable industry engineering experts and CableLabs have already established that such specifications are required for reliable digital transmission. Thus, equipment vendors and operators alike must limit their deployment to only RF DOCSIS compliant digital transmission equipment in *any* QAM application including VOD.

### 5.2.3.1 Increased interleaver depth

As seen in our discussion above and as presented in some of the test results, the interleaver depth supported by most set-tops today may not have enough margin for full dispersal of burst errors in the type of channels found in CATV. A further concern is the fact that even some QAM downstream modulator-transmitters are incapable of operating at the full depths provided in the standard. Figure 3 shows that an interleaver depth of more than 300  $\mu$ s would be required to handle CSO and CTB transients. As new and more frequency-accurate analog modulators get deployed, the spectral frequency spread of CSO and CTB components are expected to be narrower, resulting in even longer characteristic burst time, as noted in reference to Figure 4. Table 2 shows the various depth options available under J-83 Annex B. It becomes obvious that the earlier one starts to deploy full depth interleaving, head-end equipment - the better.

<i>I</i> (# of taps)	<i>J</i> (increment)	Burst protection 64-QAM/256-QAM	Latency 64-QAM/256-QAM	Comments
8	16	5.9 $\mu$ s /4.1 $\mu$ s	0.22 ms/0.15 ms	DOCSIS Requirement
16	8	12 $\mu$ s /8.2 $\mu$ s	0.48 ms/0.33 ms	
32	4	24 $\mu$ s /16 $\mu$ s	0.98 ms/0.68 ms	
64	2	47 $\mu$ s /33 $\mu$ s	2.0 ms/1.4 ms	
128	1	95 $\mu$ s /66 $\mu$ s	4.0 ms/2.8 ms	
128	2	190 $\mu$ s /132 $\mu$ s	8.0 ms/5.6 ms	
128	3	285 $\mu$ s /198 $\mu$ s	12 ms/8.4 ms	Not supported by most digital video set-tops
128	4	379 $\mu$ s /264 $\mu$ s	16 ms/11 ms	
128	5	474 $\mu$ s /330 $\mu$ s	20 ms/14 ms	
128	6	569 $\mu$ s /396 $\mu$ s	24 ms/17 ms	
128	7	664 $\mu$ s /462 $\mu$ s	28 ms/19 ms	
128	8	759 $\mu$ s /528 $\mu$ s	32 ms/22 ms	

**Table 2.** Interleaver depth settings available in J-83 Annex B.

#### 5.2.4 Secure next-generation transmitters and set-tops with specific improvements

From the deficiency list compiled in Section 5.1 above, we turn to two items:

##### 5.2.4.1 Improved Adaptive Equalizers

A particularly important feature of adaptive equalization systems employed in demodulators is their ability not only to equalize the channel frequency response by minimizing Inter-Symbol Interference (ISI), but also “equalizing-out” interference signals. In the presence of discrete interference signals, many equalizer systems are able to automatically converge to a state that forms a sharp notch at the frequency of the interferer. The degree of rejection and the speed at which these equalizers converge becomes a key attribute of the demodulator. There is no doubt that demodulator chip makers are now looking at improved equalization techniques with a particular goal of improving the narrow-band rejection capability. The author envisions industry efforts to better characterize and standardize CSO/CTB

rejection capability of demodulators so that these attributes become part of a qualification or certification process.

## 6 Summary and Conclusions

There is reason to review and substantially revise the required margins for reliable 256 QAM operations. It is argued that composite distortion terms having envelope peaks that can reach up to 16 dB above their average level leave very little room for further noise degradations at *any* level of the signal distribution. First-order statistics for CSO and CTB envelopes were simulated and specific degradations due to various factors including shorter interleaver spans were analyzed. Finally various mitigation steps have been recommended in order to enable successful rollout of 256 QAM.

## 7 Acknowledgement

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